

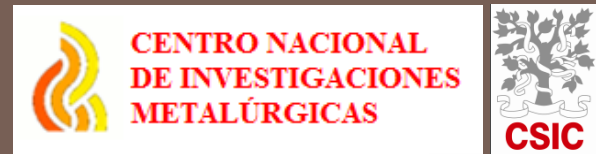
# DETERMINATION OF GRAIN BOUNDARY MOBILITY IN THE FE-CR SYSTEM BY MOLECULAR DYNAMICS SIMULATION

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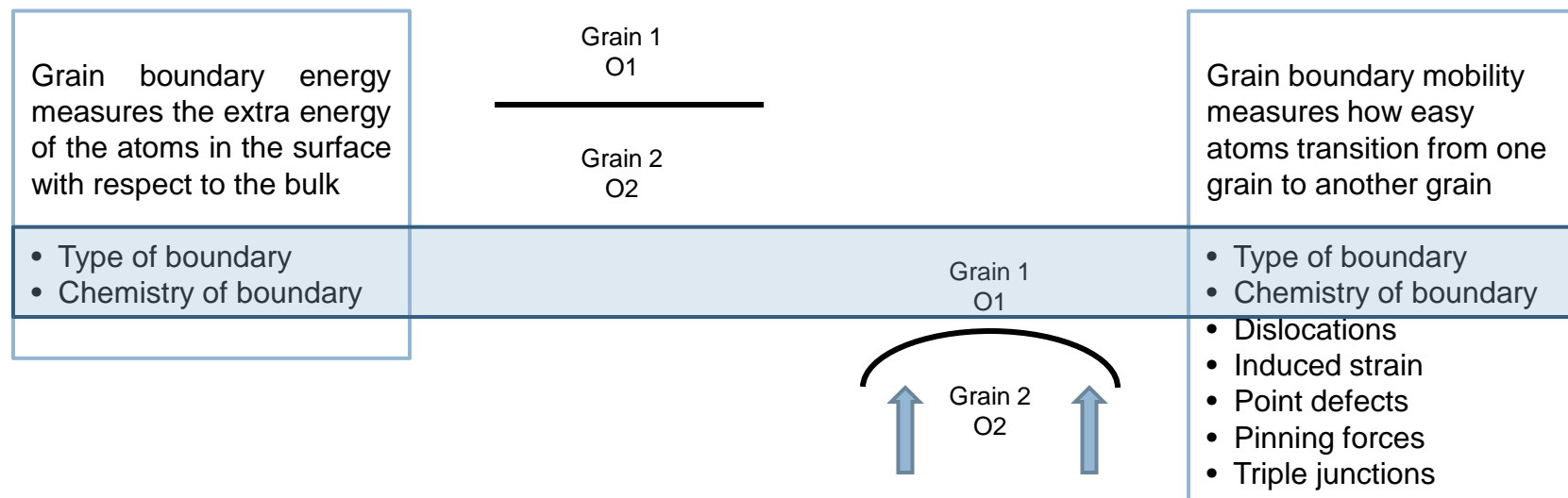
<sup>2</sup>Department of Materials Science and Metallurgy, (Cambridge University-UK)

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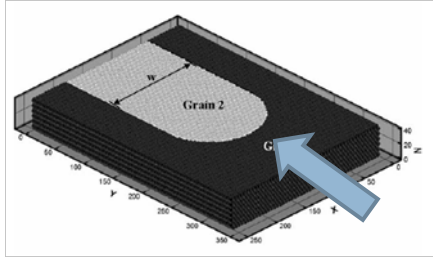
- Introduction
  
- Model Setup
  - ▣ Molecular Dynamics
  - ▣ Simulating Grain Boundary Mobility
  - ▣ Grain Boundary Characteristics
  
- Simulation Results
  
- Conclusions and Questions

# Introduction

- We have deal with the problem of recrystallisation of oxide dispersion strengthened Fe-Cr (ODS).
  - ▣ Exceptional high recrystallisation temperatures (0.9 of melting temperature)
  - ▣ Extremely coarse final grains, some orders of magnitude bigger than the initial microstructure
- Many different recrystallisation simulations try to explain the behaviour of grain growth and migration
  - ▣ Cellular automata, Monte Carlo, Finite Element Modelling, Vertex, ...
- Grain boundary energy vs. Grain boundary Energy + Mobility

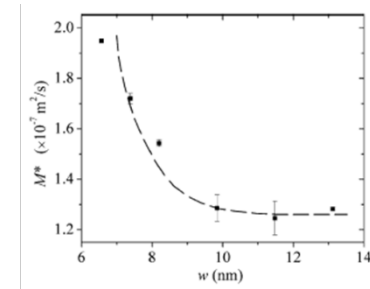
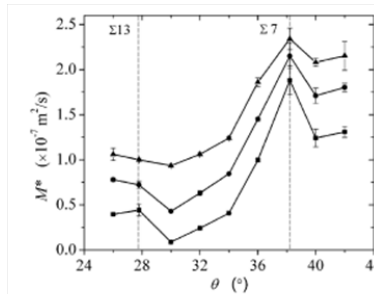


# Introduction

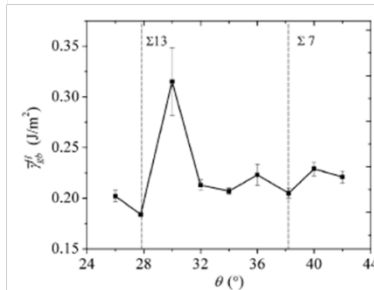


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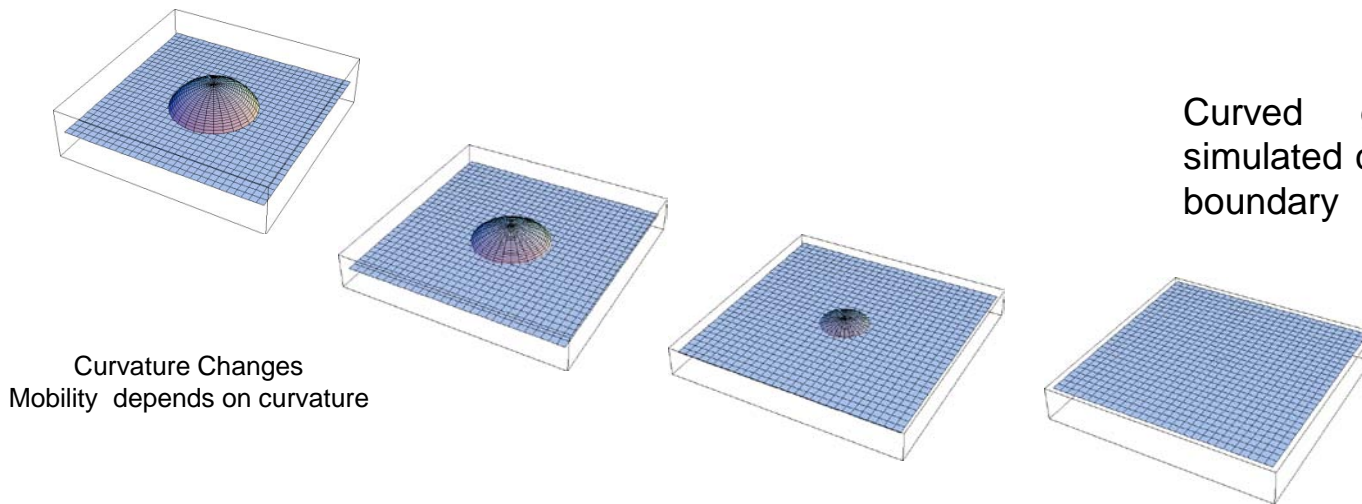
$$v = M(\gamma_{gb} + \gamma''_{gb}) \left( \frac{\pi}{w} \right) = M^* \left( \frac{\pi}{w} \right)$$



Curvature Constant  
Mobility does not  
depend on curvature



Curved grain boundary  
simulated closer to flat grain  
boundary



Curvature Changes  
Mobility depends on curvature

# Molecular Dynamics

- The classical approach of Finnis-Sinclair has been used to compute the movement of atoms
  - Good fitting with physical and mechanical properties of iron and chromium. BCC structure
    - Fe cell parameter is 2.8665 Å. Cohesive energy per atom of -4.28eV
    - Cr cell parameter is 2.8845 Å. Cohesive energy per atom of -4.10eV
  - It has been successful in modeling defects of surfaces, interactions between atoms and for calculating grain boundary energies.
  - The parameters for the pairs Fe-Fe and Cr-Cr has been chosen from the original work of Finnis and Sinclair [1-2] and for the Fe-Cr interactions, the Lorentz-Berthlot rule has been used.

## Finnis-Sinclair Potential

$$E = \frac{1}{2} \sum_i \sum_j V_{ij}(r_{ij}) - A \sum_i \sqrt{\rho_i}$$

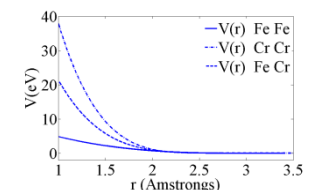
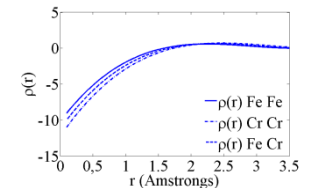
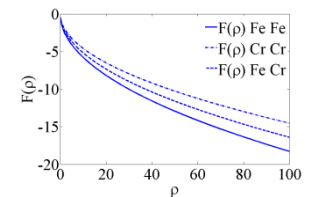
$$V_{ij}(r) = \begin{cases} (r-c)^2(c_0 + c_1 r + c_2 r^2) & \text{si } (r \leq c) \\ 0 & \text{si } (r > c) \end{cases}$$

$$\rho_i = \sum_{i \neq j} \phi(r_{ij})$$

$$\phi(r) = \begin{cases} (r-d)^2 + \beta \frac{(r-d)^3}{d} & \text{si } (r \leq d) \\ 0 & \text{si } (r > d) \end{cases}$$

## Lorentz-Berthlot mixing rule

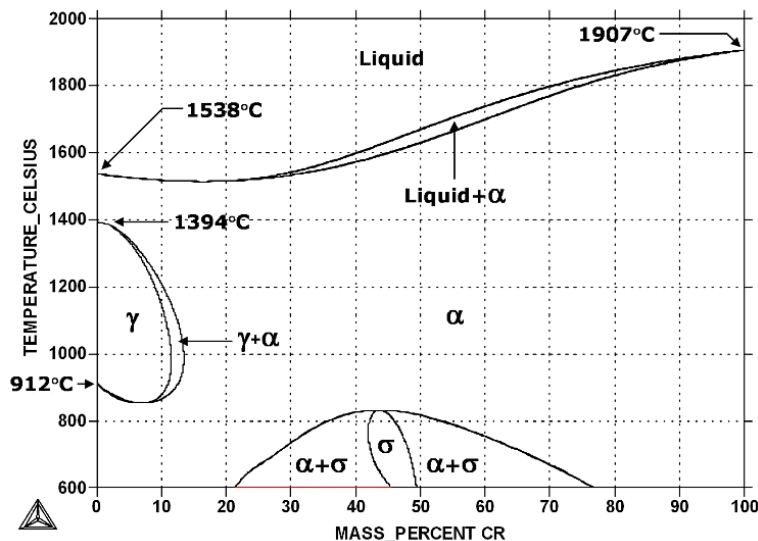
$$\left\{ \begin{array}{l} c^{FeCr} = \frac{c^{Fe} + c^{Cr}}{2} \\ \beta^{FeCr} = \frac{\beta^{Fe} + \beta^{Cr}}{2} \\ c_0^{FeCr} = \sqrt{c_0^{Fe} \cdot c_0^{Cr}} \\ c_2^{FeCr} = \frac{c_2^{Fe} \cdot c_0^{Cr} + c_2^{Cr} \cdot c_0^{Fe}}{2\sqrt{c_0^{Fe} \cdot c_0^{Cr}}} \end{array} \right\} \left\{ \begin{array}{l} d^{FeCr} = \frac{d^{Fe} + d^{Cr}}{2} \\ A^{FeCr} = \frac{A^{Fe} + A^{Cr}}{2} \\ c_1^{FeCr} = \frac{c_1^{Fe} \cdot c_0^{Cr} + c_1^{Cr} \cdot c_0^{Fe}}{2\sqrt{c_0^{Fe} \cdot c_0^{Cr}}} \end{array} \right\}$$



$c$  represents a *cutoff* parameter,  $c_1$ ,  $c_2$ ,  $c_3$  are fitting parameters,  $d$  is a different *cutoff* parameter,  $A$  binding energy

# Molecular Dynamics

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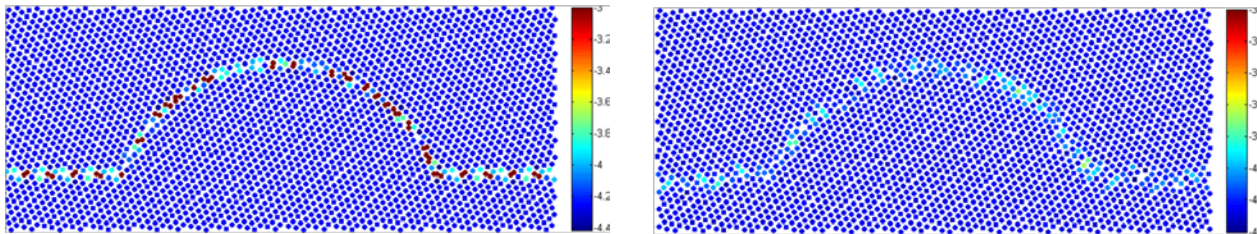
Cohesive energy in BCC is -4.28 eV ( $a=2.8665 \text{ \AA}$ )  
 Cohesive energy in FCC is -4.23 eV ( $a=3.6938 \text{ \AA}$ )

$BCC_E < FCC_E$  independently of temperature so it is difficult to simulate with this potential phase transformation.

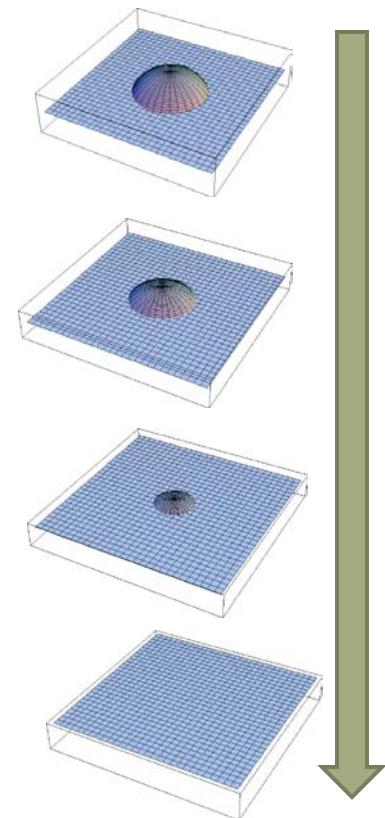
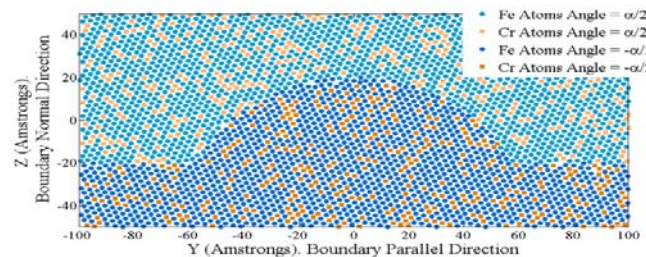
No allotropic phase transformation has been seen in FS potential  
 Fe-20Cr has no phase transformation.

# Simulating Grain Boundary Mobility

- Grain boundary energy is computed by setting up two different orientations and defining a connecting plane
  - No curvature => No curvature driven mobility measurement is possible
  - The initial configuration of the grain boundary energy computations are not able to say anything about mobility.
- We need a curved boundary to have a pressure on the surface.



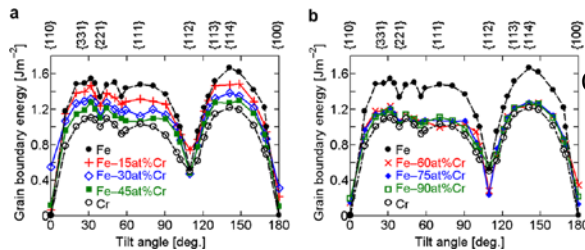
$$S_i = \frac{\sum_j \cos((k \cdot r_i - k \cdot r_j)/a 2\pi)}{n^2}$$



$$v = M \cdot P \quad ; \quad M = M_0 \exp(-Q/kT) \quad ; \quad P = \frac{\gamma_{gb} + \gamma_{gb}}{R} \quad ; \quad v = M \cdot \frac{\gamma_{gb} + \gamma_{gb}}{R} = M^* \frac{1}{R}$$

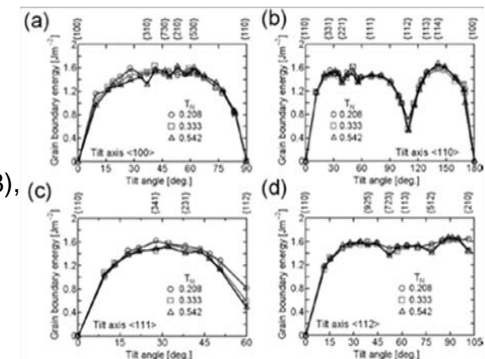
# Grain Boundary Choice

- <110> Symmetric Tilt Grain boundary:
  - Mechanically alloyed metals has in general has a <110> fiber tilt boundary characteristics
  - Obviously it can be represented LAGB and HAGB
  - CSL nomenclature (coincident site lattice) has influence in some cases
    - It is of paramount importance in some specific cases, although in general LAB or HAB have higher effect on grain boundary properties.
  - In general tilt boundaries (symmetric or asymmetric) are the most common boundaries
    - Symmetrical tilt boundaries are very useful for molecular dynamic simulations. Easy boundary conditions
  - We have previous information about this family



Y. Shibuta, et al.  
Computational Materials  
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International, Vol. 48 (2008),  
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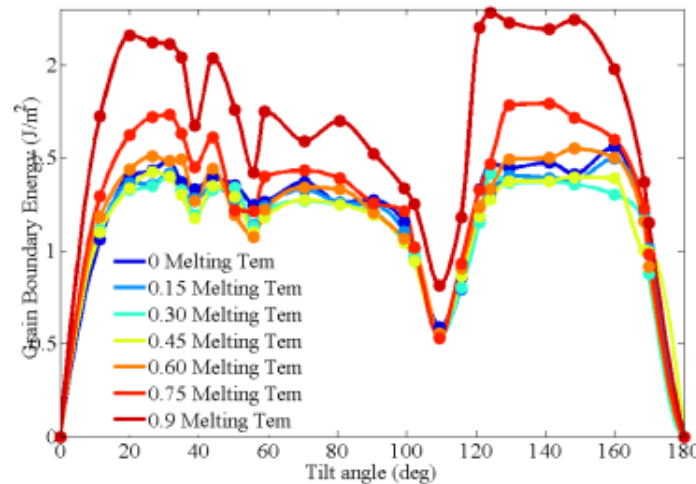
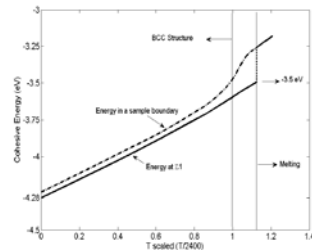




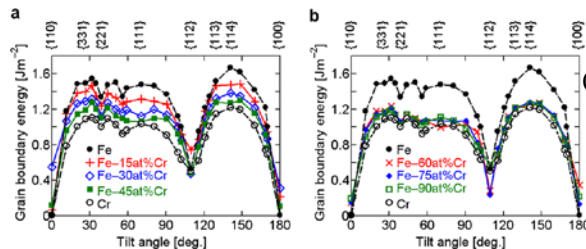
# Grain Boundary Choice

□ <110> Symmetric Tilt Grain boundary:

$$\gamma = \frac{E_{\text{tot}} - CE(T) \cdot N_{\text{atoms}}}{2 \cdot A}$$

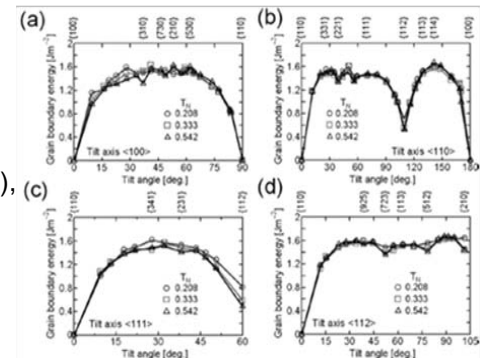


## Grain Boundary Energy in the Fe-20%Cr system with respect to Misorientation and Temperature



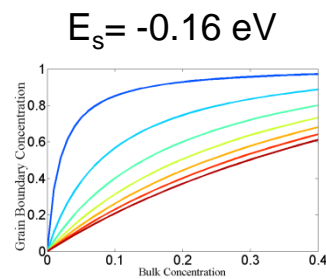
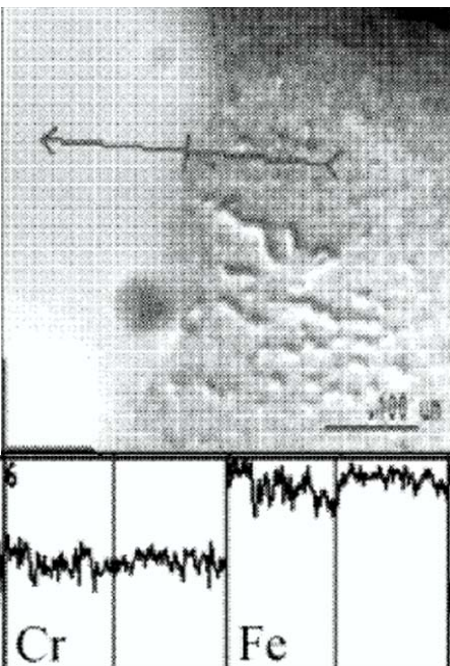
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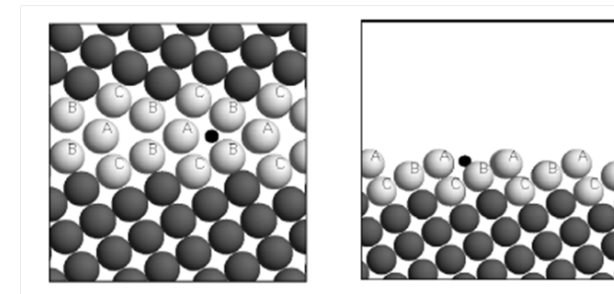
# Grain Boundary Set Up

- Segregation must be considered if two different kind of atoms are involved
  - Why ? ..... Previous evidences in very pure system (Al), just a little amount of impurities can affect drastically the mobility
    - 99.9992 % Al is two orders of magnitude lower than 99.99995 %Al
  - Experimental results on mechanically alloyed metals did not detect segregation in the boundary or in the bulk
    - High recrystallization temperature
    - Kinematics of diffusion are slower than cooling process
    - Similar atoms Fe-Cr. Other “less” similar atoms can affect
    - Oxide particles
    - Predominant Low angle misorientation
    - ...



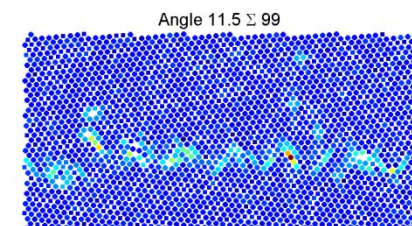
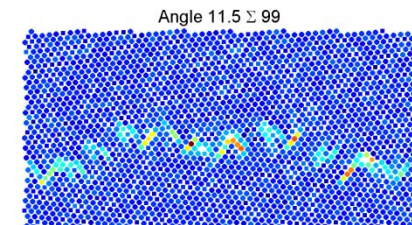
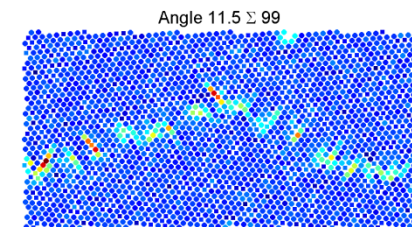
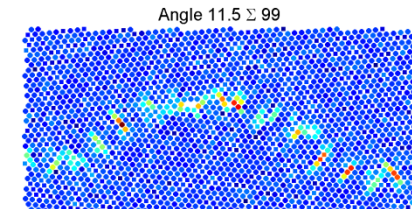
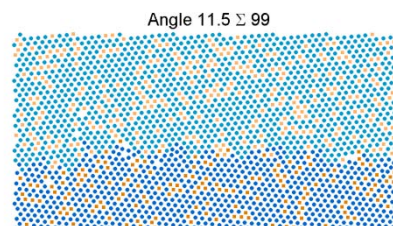
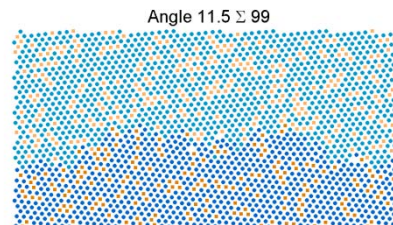
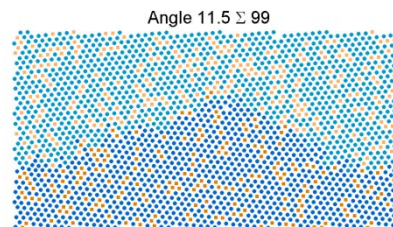
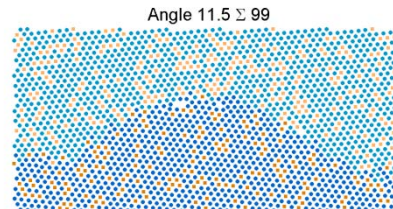
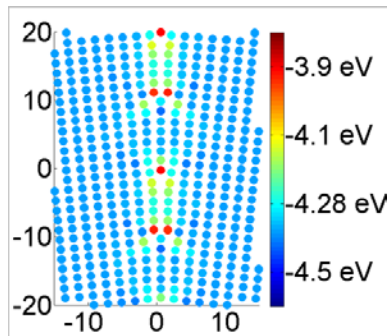
$$C_d = \frac{C \cdot e^{E_s/kT}}{1 - C + C \cdot e^{E_s/kT}}$$

Site of Substitutional Impurity		Cr
Site A	boundary	-0.220
	surface	-0.560
Site B	$E_{\text{surf}} - E_{\text{bound}}$	-0.340
	boundary	-0.170
	surface	-0.560
Site C	$E_{\text{surf}} - E_{\text{bound}}$	-0.390
	boundary	-0.100
	surface	-0.340
$E_{\text{surf}} - E_{\text{bound}}$		-0.240



# Simulation Results

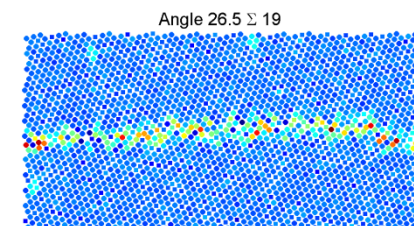
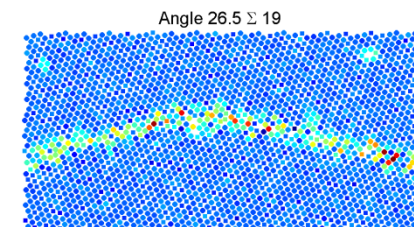
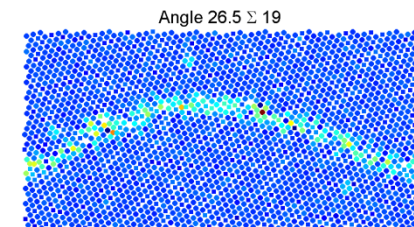
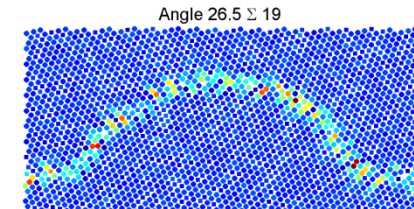
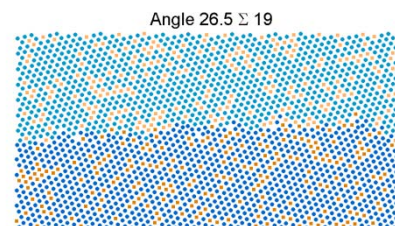
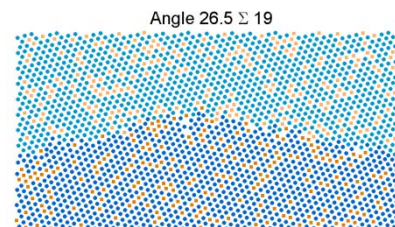
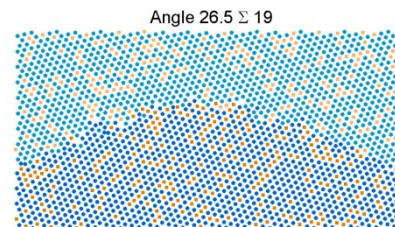
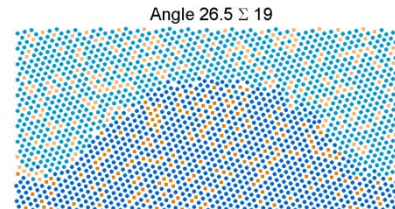
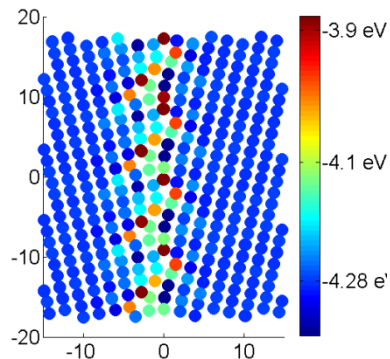
- Case 11.5°
  - Low mobility
    - $M^* = 4 \text{ E}^{-9} \text{ m/s}^2$
  - High Activation Energy
    - $Q = 1.25 \text{ eV}$
  - Low grain boundary energy
    - $\gamma = 1 \text{ J/m}^2$
- Grain boundary structure



# Simulation Results

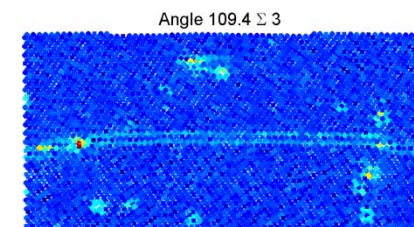
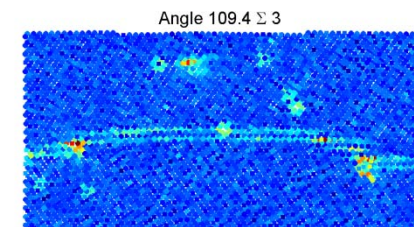
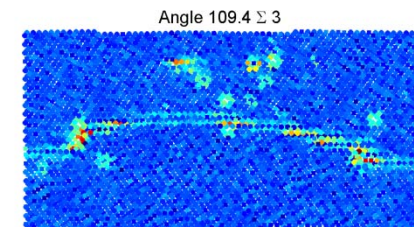
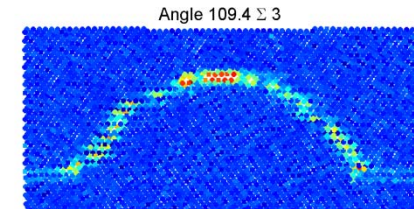
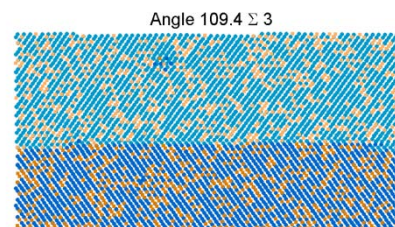
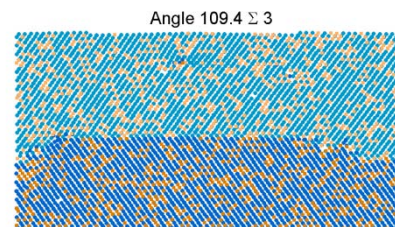
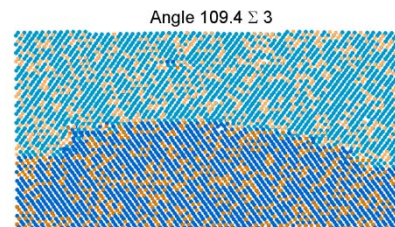
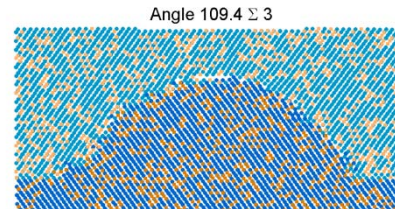
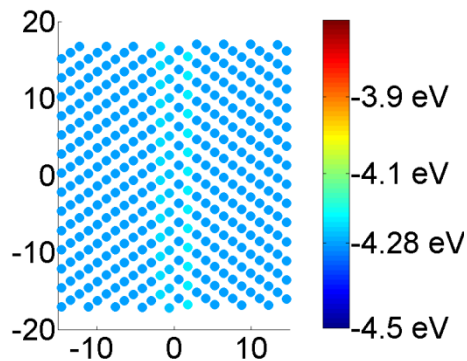
- Case 26.5°
  - High Mobility
    - $M^* = 9 E^{-9} \text{ m/s}^2$
  - Low Activation Energy
    - $Q = 0.61 \text{ eV}$
  - High grain boundary energy
    - $\gamma = 2.2 \text{ J/m}^2$

- Grain boundary structure



# Simulation Results

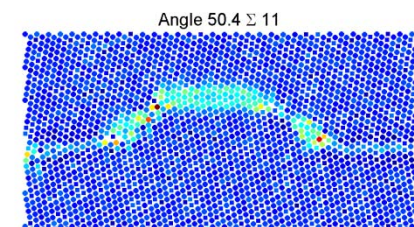
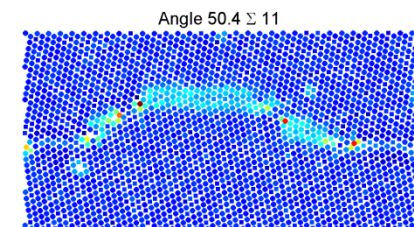
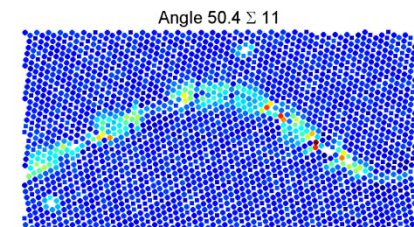
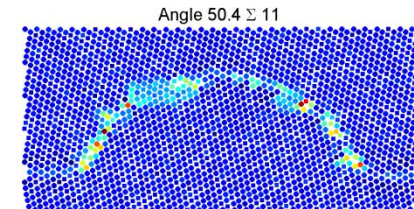
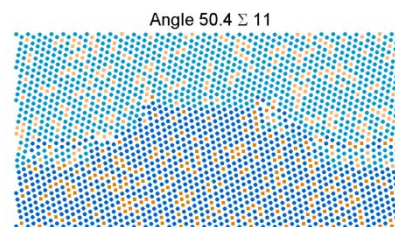
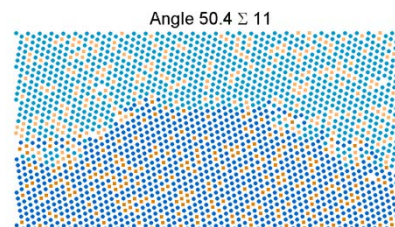
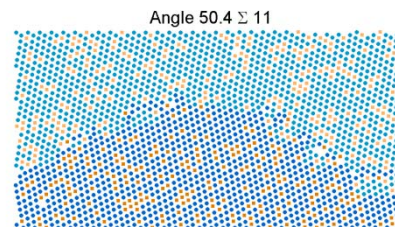
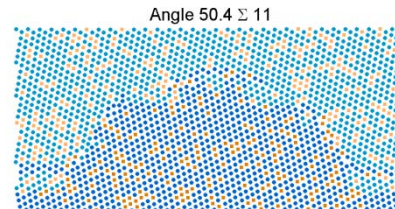
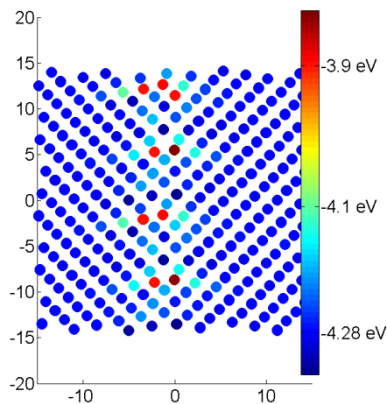
- Case 109°
  - Very High mobility
    - $M^* = 15 E^{-9} \text{ m/s}^2$
  - Very Low Activation Energy
    - $Q = 0.27 \text{ eV}$
  - Low grain boundary energy
    - $\gamma = 0.7 \text{ J/m}^2$
  
- Grain boundary structure



# Simulation Results

- Case 50.4°
  - Low mobility
    - $M^* = 2.4 \text{ E}^{-9} \text{ m/s}^2$
  - Medium Activation Energy
    - $Q = 0.71 \text{ eV}$
  - High grain boundary energy
    - $\gamma = 1.7 \text{ J/m}^2$

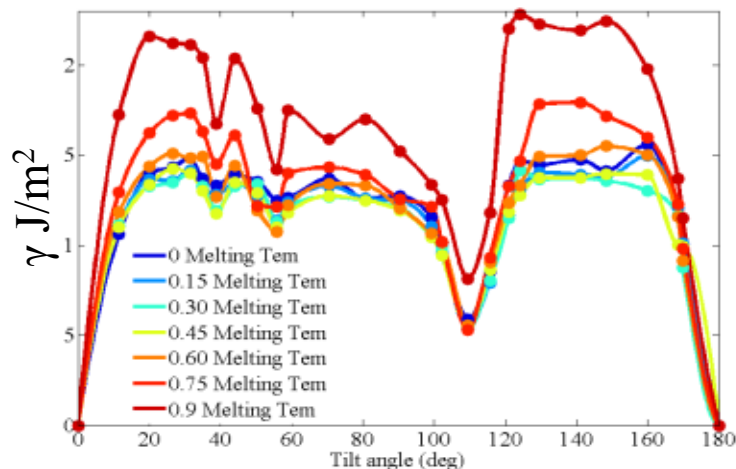
- Grain boundary structure



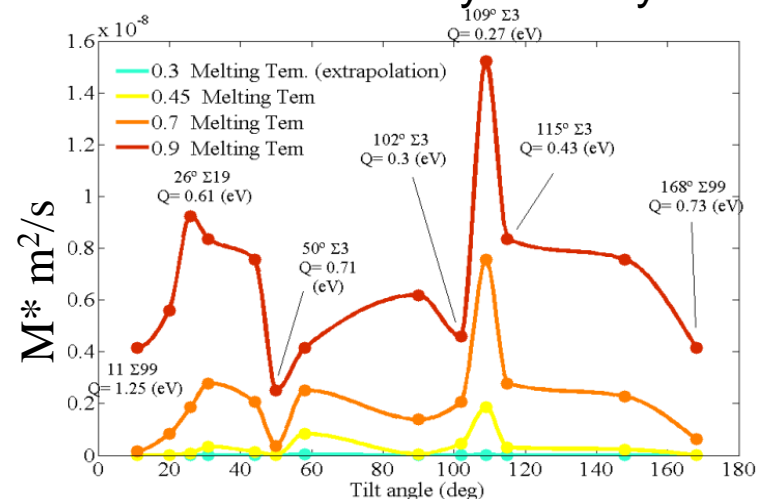
# Simulation Results

- We have computed a set of representative boundaries for three different medium and high temperatures

<110> symmetric tilt  
Grain boundary energy



<110> symmetric tilt  
Grain Boundary Mobility



A Previous work [1] reports similar mobility in ODS PM2000 (Fe-20Cr-5Al) , although an activation energy significantly higher than simulations:

# Conclusions

- ❑ Hat-shape geometry has been tested to compute mobility in the Fe-Cr system without segregation in the boundaries
- ❑ LAGB has in general lower mobility than HAGB
- ❑ But LAGB / HAGB classification is not enough to classify the mobility of a boundary
  - Configuration of atoms affects mobility as well as affects grain boundary energy
  - Low energy in HAGB has very high mobility
  - Some HAGB behave as LAGB
- ❑ It seems to be a relationship between grain boundary energy and mobility
- ❑ Previous works [1] report similar mobility in ODS PM2000 (Fe-20Cr-5Al), although an activation energy significantly higher than simulations:
  - Pinning particles
  - more elements
  - texture dominated by LAGB
- ❑ Future work
  - Comparison with U-shape bicrystal geometry
  - Stress induced mobility
  - Longer simulations with segregation at the boundaries
  - Effect of Dislocations and vacancies
  - More elements (Al)
  - ...

Thank you for  
your attention

