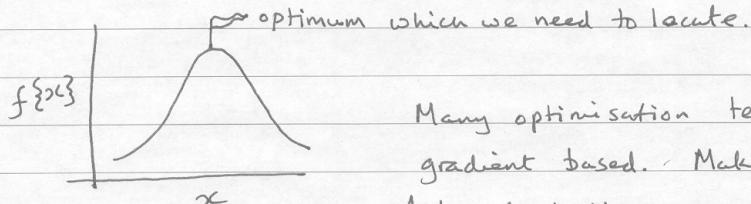


## Genetic Algorithms - Lecture ①

We will be using biological terms to introduce the subject, focusing on fundamentals rather than applications.

Will use genetic algorithms for optimisation problems.



Many optimisation techniques are gradient based. Make a guess, take derivatives, and hence find maximum when slope = 0

Genetic algorithm uses a non-calculus method instead, i.e., it is not necessary to take derivatives. Instead of just one guessed value, begin with many.

Simple algorithm      Guessed value  $\rightarrow$  several

Each guessed value is an "individual"

Set of guessed values is a "population"

$f\{\vec{x}_i\} = f\{x_1, x_2, x_3, \dots\}$	<table border="0"> <tr> <td><math>x_4</math></td><td><math>x_3</math></td><td><math>x_2</math></td><td><math>x_1</math></td></tr> <tr> <td>1 0 0</td><td>1 0 0</td><td>1 0 0</td><td>1 1 0</td></tr> <tr> <td><math>\vec{x}_4</math></td><td><math>\vec{x}_3</math></td><td><math>\vec{x}_2</math></td><td><math>\vec{x}_1</math></td></tr> </table>	$x_4$	$x_3$	$x_2$	$x_1$	1 0 0	1 0 0	1 0 0	1 1 0	$\vec{x}_4$	$\vec{x}_3$	$\vec{x}_2$	$\vec{x}_1$	individual guess
$x_4$	$x_3$	$x_2$	$x_1$											
1 0 0	1 0 0	1 0 0	1 1 0											
$\vec{x}_4$	$\vec{x}_3$	$\vec{x}_2$	$\vec{x}_1$											
	<table border="0"> <tr> <td>1 1 0</td><td>1 0</td><td>1 1 1</td><td>1 0 0</td> </tr> <tr> <td><math>\vec{x}_4</math></td><td><math>\vec{x}_3</math></td><td><math>\vec{x}_2</math></td><td><math>\vec{x}_1</math></td> </tr> </table>	1 1 0	1 0	1 1 1	1 0 0	$\vec{x}_4$	$\vec{x}_3$	$\vec{x}_2$	$\vec{x}_1$	another individual guess				
1 1 0	1 0	1 1 1	1 0 0											
$\vec{x}_4$	$\vec{x}_3$	$\vec{x}_2$	$\vec{x}_1$											
	⋮													

Variables are mapped onto a binary number above

Where do we get the binary strings? To begin with at random, a random sequence of 1 and 0's.

How do the binaries represent real numbers? By linear mapping

$$\text{Suppose we wish to decode } 11001 \equiv 1 \times 2^0 + 0 \times 2^1 + 0 \times 2^2 + 1 \times 2^3 + 1 \times 2^4 \\ \text{begin here} \quad = \text{real number} = s_i$$

However, linear mapping is different!

Suppose the decoded integer value is  $s_i$

$$s_i = \text{decoded value}$$

Suppose  $x_i^{\text{upper}}$ , maximum value of  $x_i$ , is provided by user.

Similarly  $x_i^{\text{lower}}$ , also given

Then provide another quantity  $l$ , the length of the binary string.

Once this is done, linear variable mapping is simple

If real value (say 32.1) is  $x_i$ , then

$$x_i = x_i^{\text{lower}} + \frac{x_i^{\text{upper}} - x_i^{\text{lower}}}{2^l - 1} (s_i) \quad \therefore \text{eqn. 1}$$

$$(s_i)_{\text{minimum}} = 00000 \quad \text{for } l=5$$

$$(s_i)_{\text{maximum}} = 11111 \quad \text{for } l=5$$

Equation 1 then provides a mapping between  $x_i$  and  $s_i$

The choice of  $l$  is related to accuracy. A larger  $l$  will give greater accuracy, but too large a value increases the computing time.

In equation 1,  $\frac{x_i^{\text{upper}} - x_i^{\text{lower}}}{2^l - 1}$  is known as

"accuracy". To select  $l$ , we make this accuracy small -

In a multivariate problem, each variable is individually mapped.

So, what is genetic about all this? We talk of "individuals".

		height	skin colour	eye colour	
individual	$f(\vec{x})$	1 0 0	1 0 0	1 0 0	*
individual		0 1 1	1 0 0	0 0 0	