

Problems in the Calculation of Transformation Texture

www.msm.cam.ac.uk/phase-trans

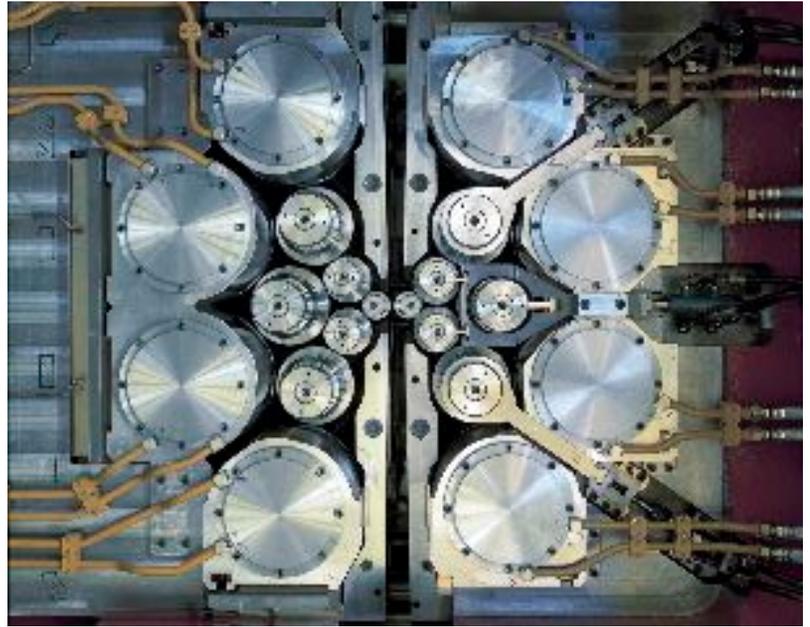
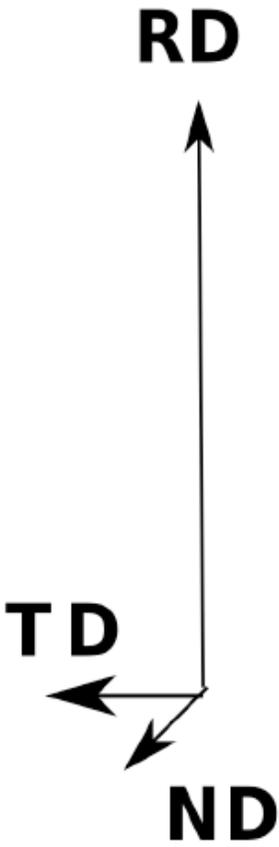
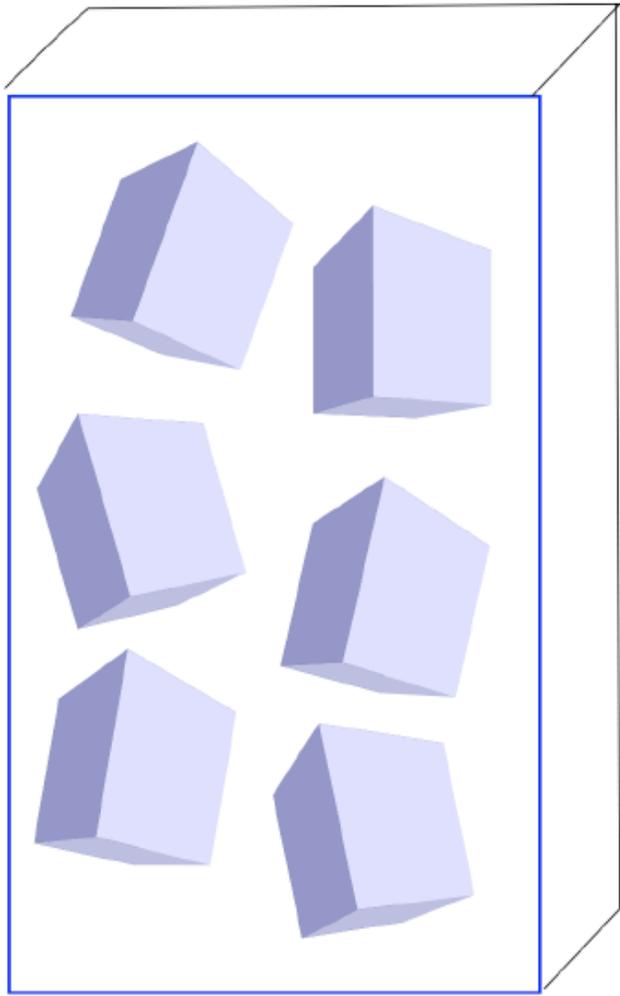
POSTECH

GIFT

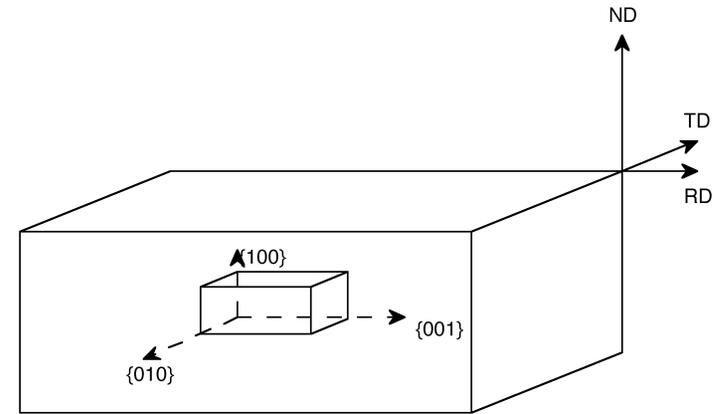
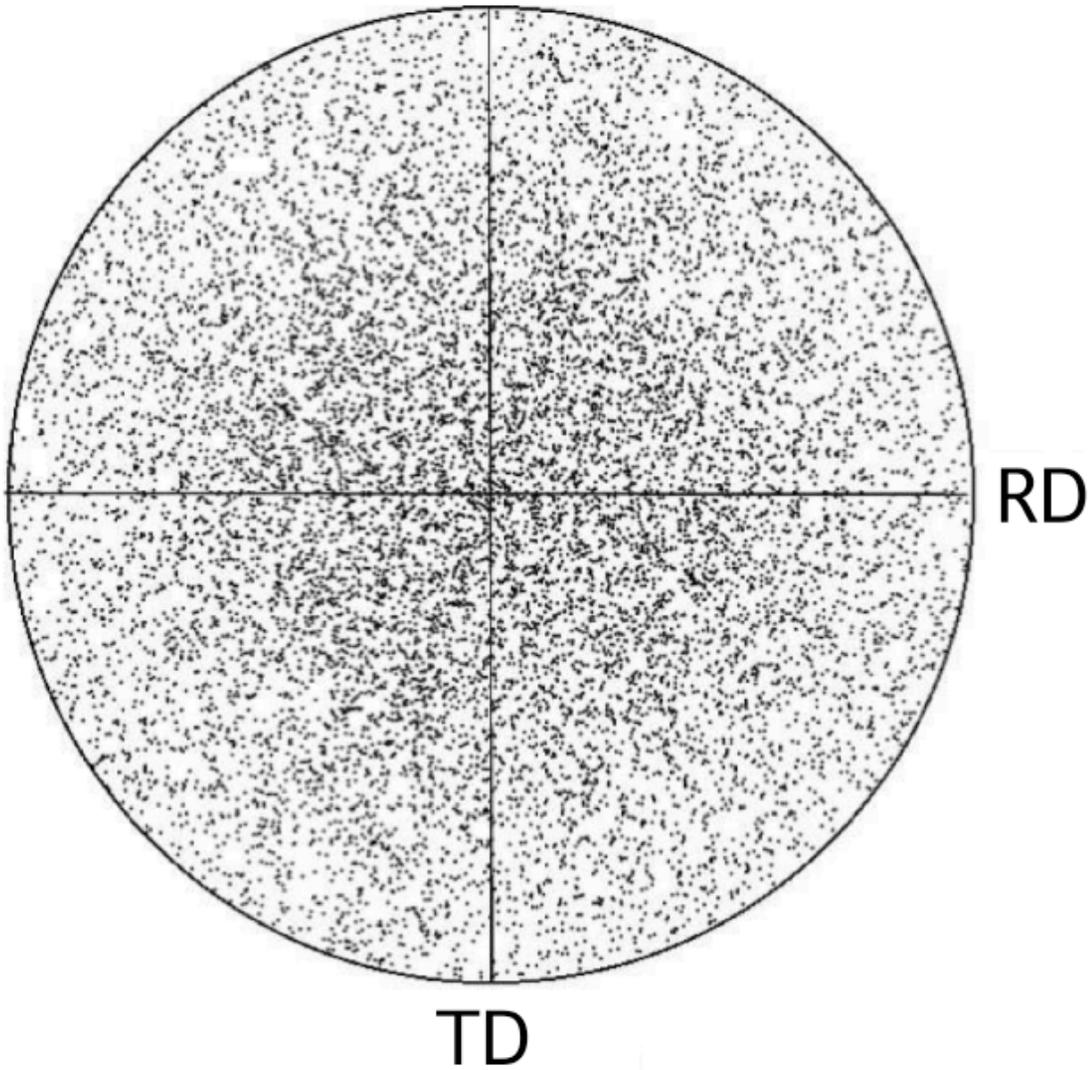
Graduate Institute of Ferrous Technology

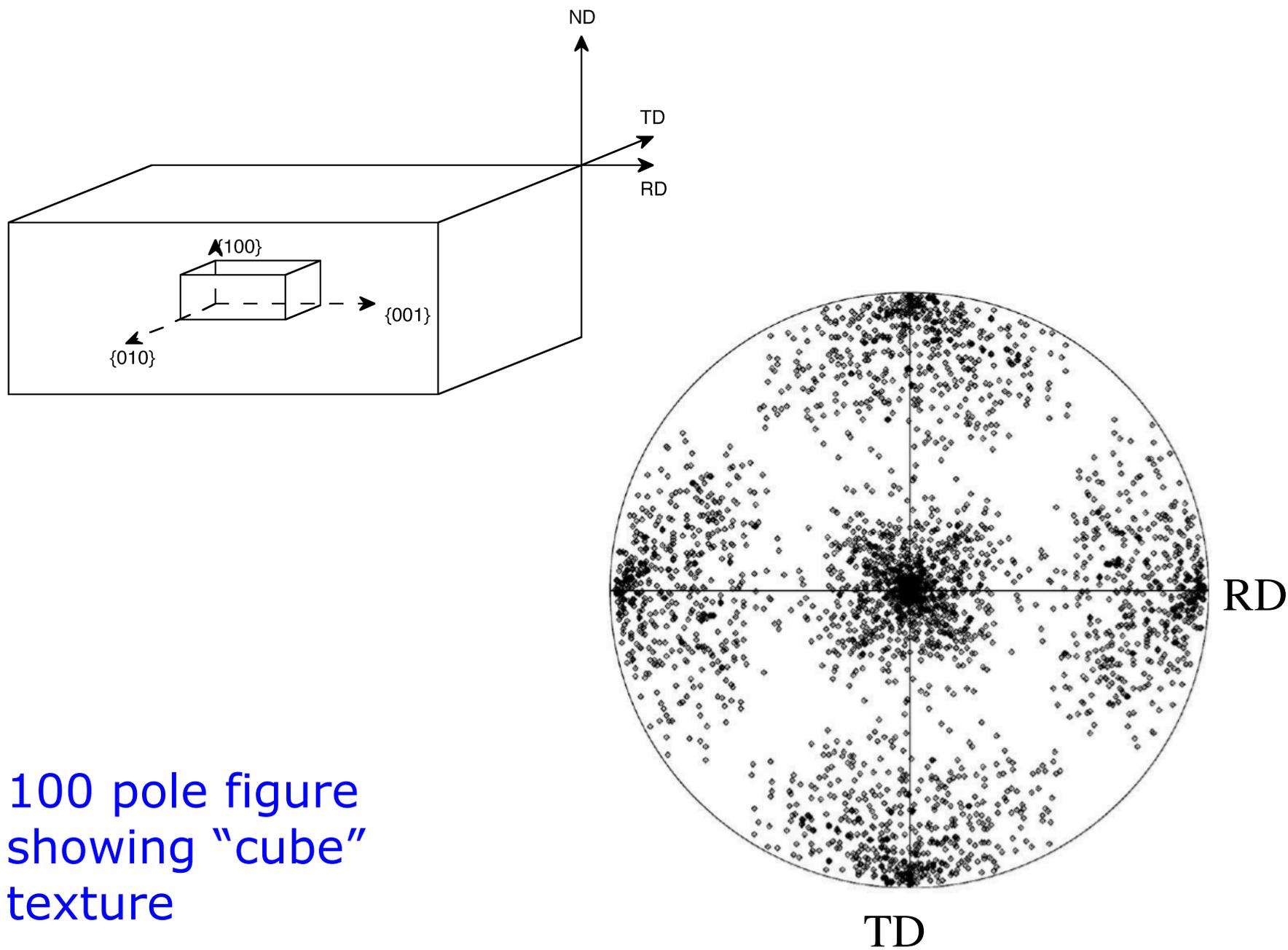


UNIVERSITY OF
CAMBRIDGE



100 pole figure plotted relative to sample axes





100 pole figure
showing "cube"
texture

RECONSTRUCTIVE

Diffusion of all atoms during nucleation and growth.
Sluggish below about 850 K.

DISPLACIVE

Invariant-plane strain shape deformation with large shear component.
No iron or substitutional solute diffusion.
Thin plate shape.

ALLOTRIOMORPHIC
FERRITE

IDIOMORPHIC
FERRITE

MASSIVE FERRITE

No change in bulk composition.

PEARLITE

Cooperative growth of ferrite & cementite.

WIDMANSTÄTTEN
FERRITE

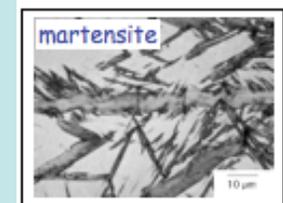
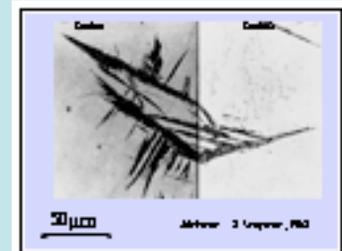
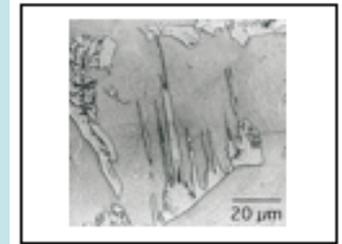
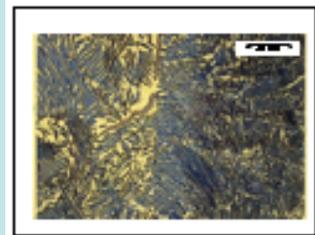
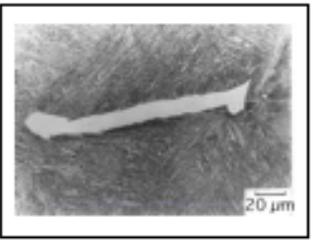
Carbon diffusion during paraequilibrium nucleation & growth.

BAINITE & ACICULAR
FERRITE

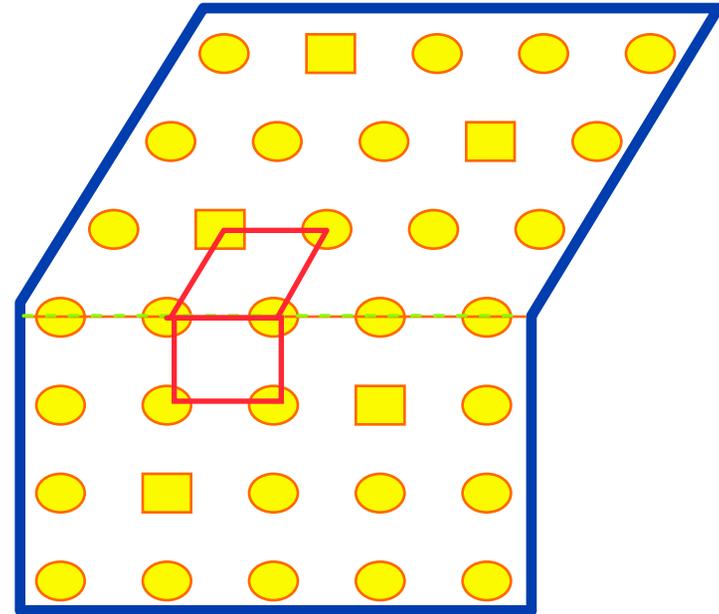
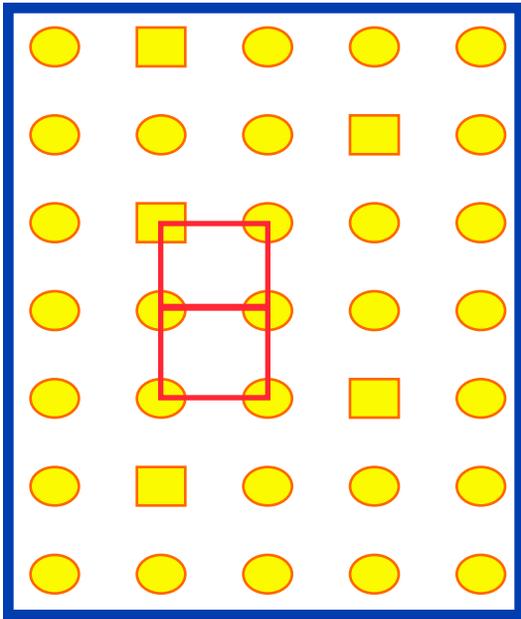
Carbon diffusion during paraequilibrium nucleation. No diffusion during growth.

MARTENSITE

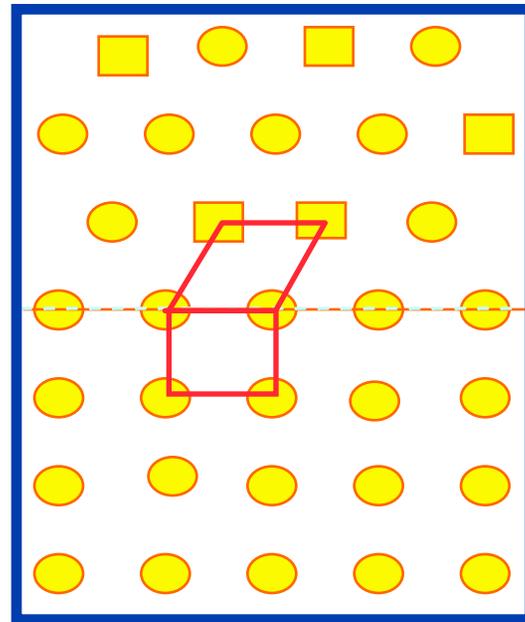
Diffusionless nucleation & growth.

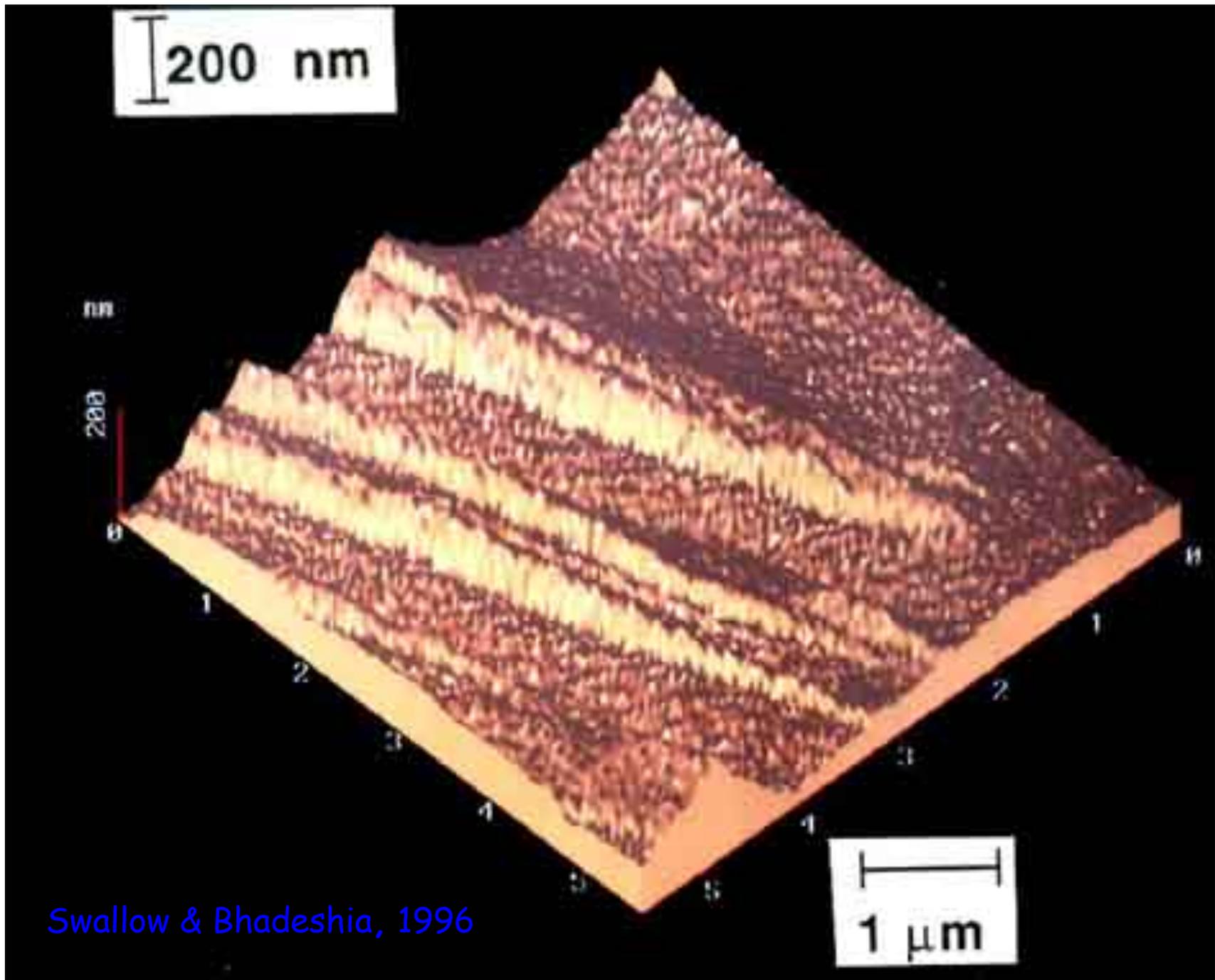


DISPLACIVE



RECONSTRUCTIVE



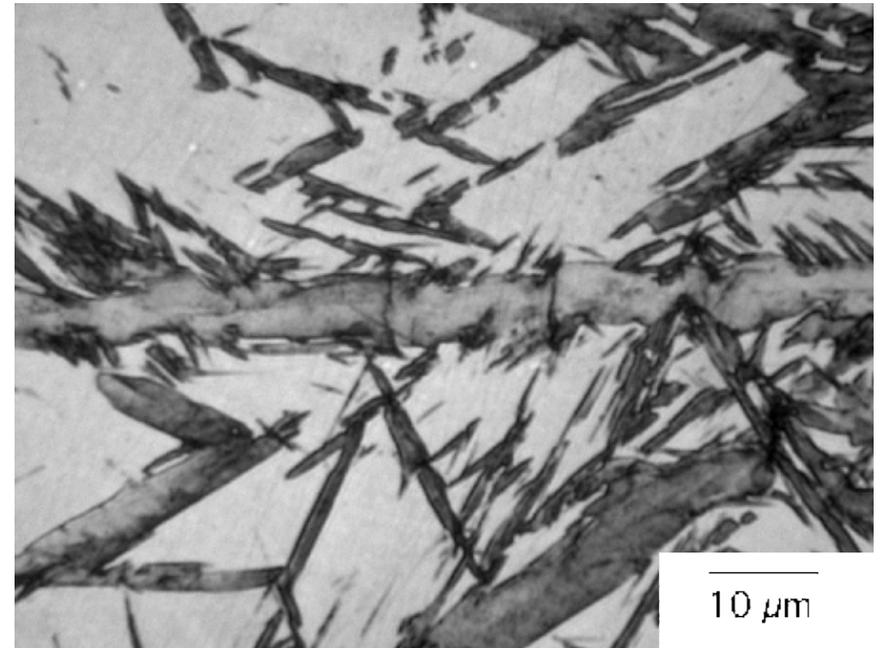
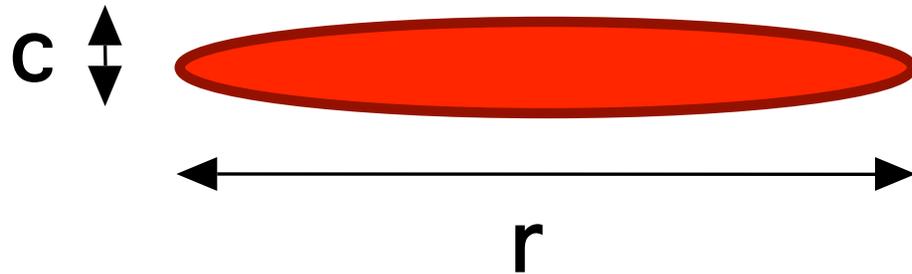


Swallow & Bhadeshia, 1996

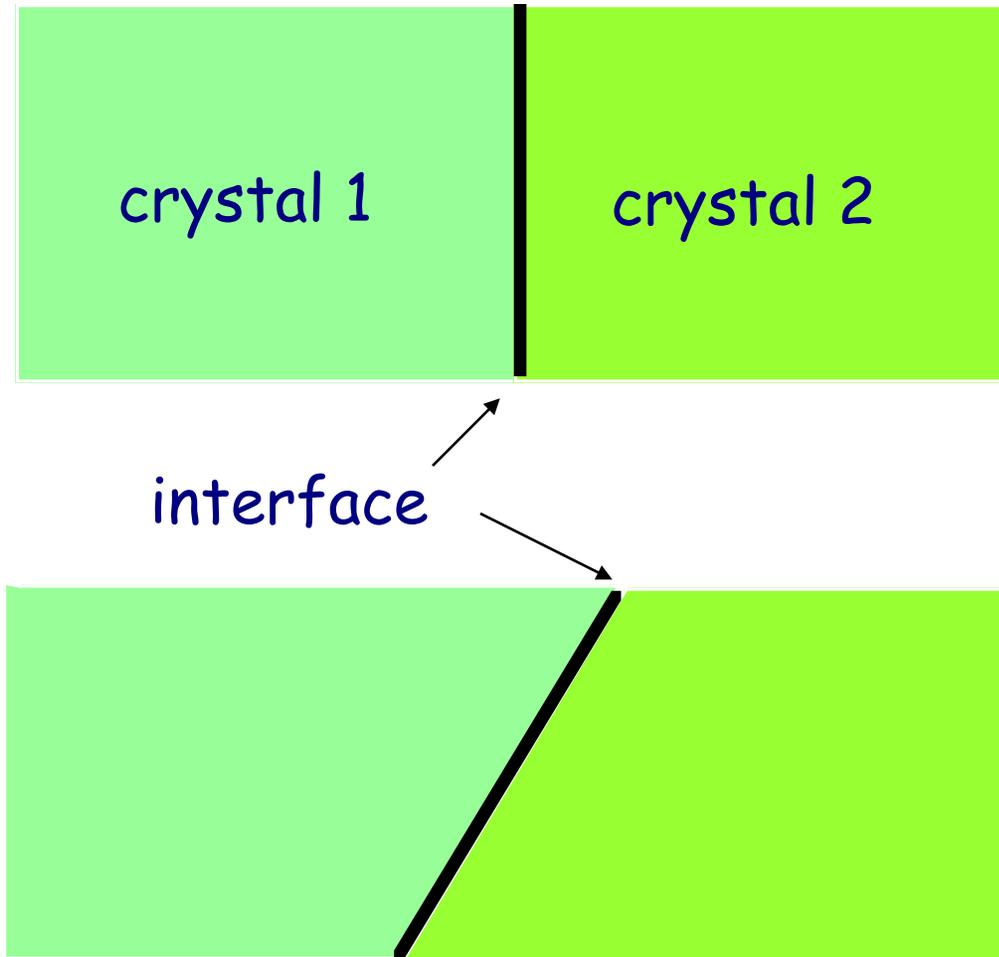
habit plane

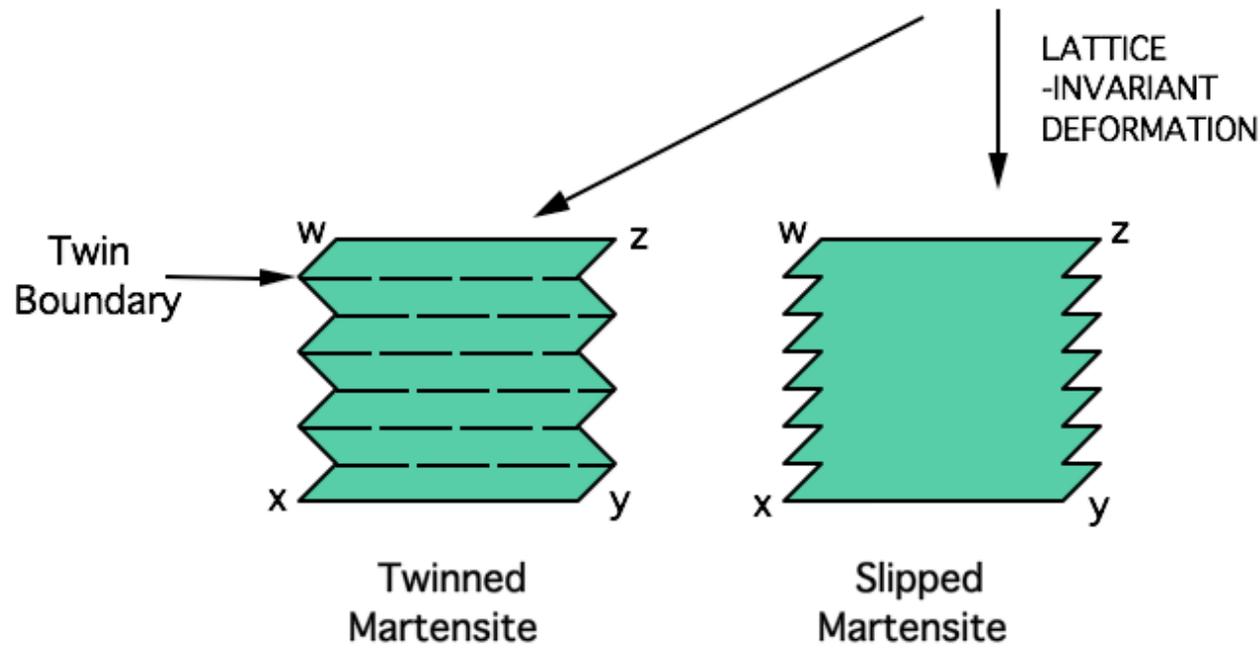
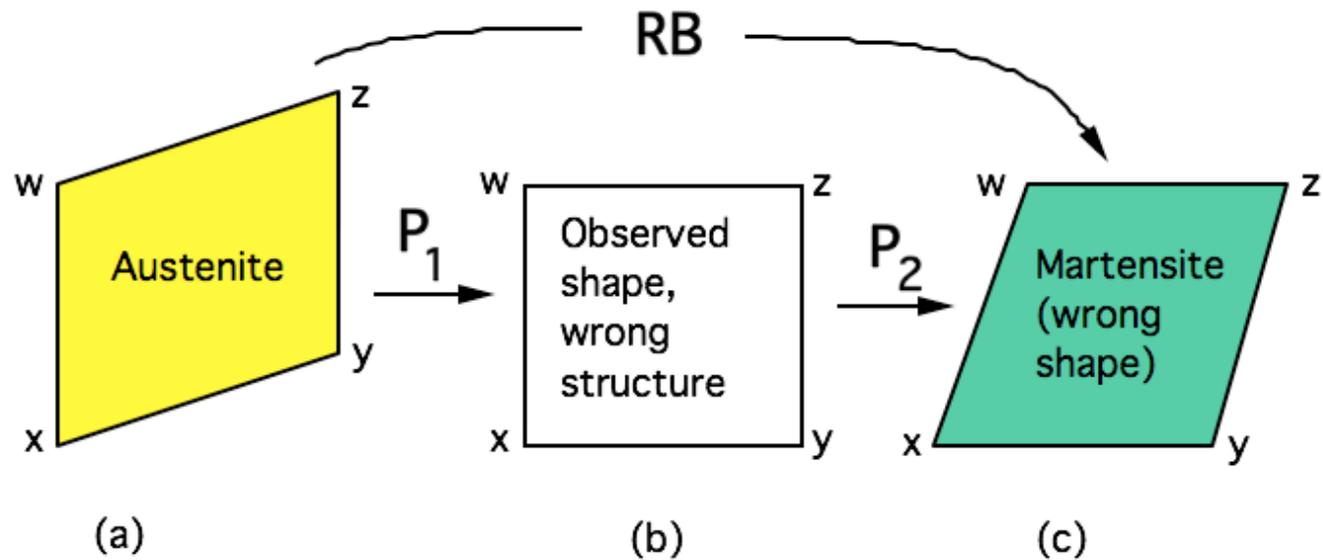
orientation relationship

deformation



Degrees of freedom





Correct macroscopic shape, correct structure

Habit plane \mathbf{p}_γ

$$\begin{pmatrix} -0.168640 \\ -0.760394 \\ -0.627185 \end{pmatrix}$$

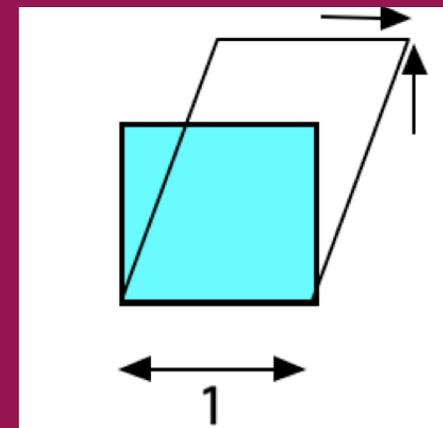
Orientation (γ J α)

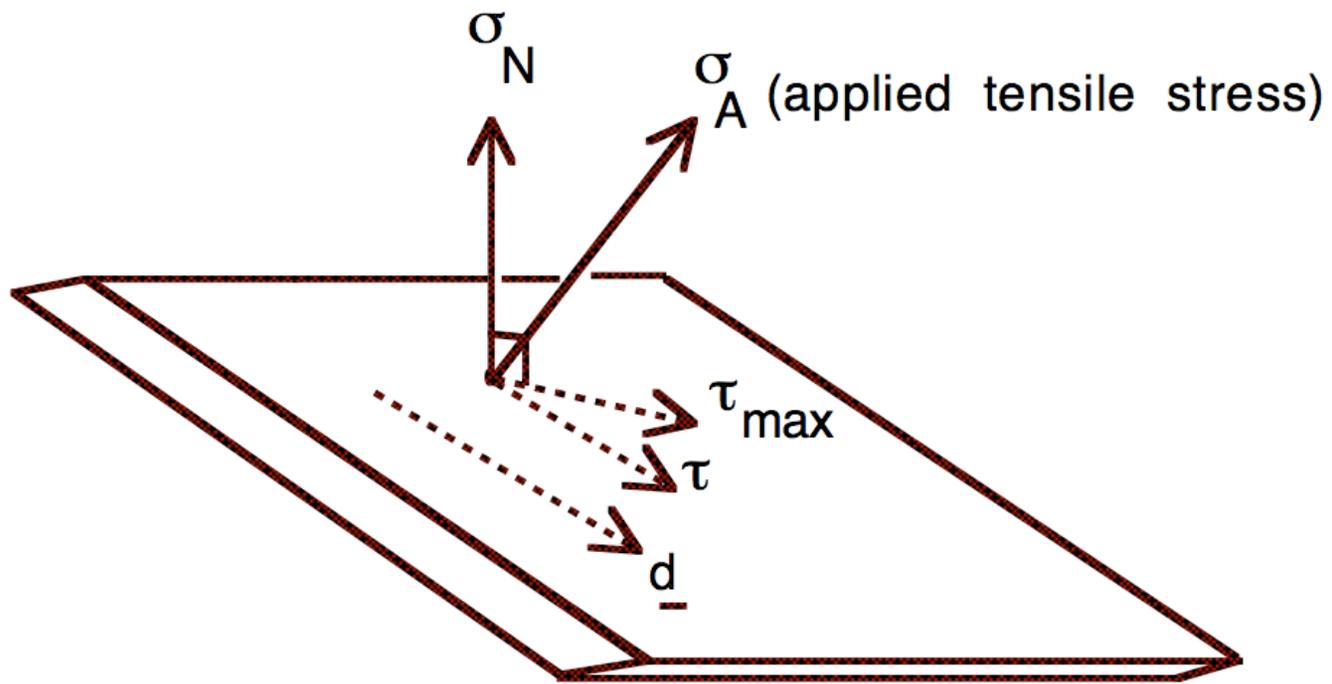
$$\begin{pmatrix} 0.575191 & 0.542067 & 0.097283 \\ -0.550660 & 0.568276 & 0.089338 \\ -0.008610 & -0.131800 & 0.785302 \end{pmatrix}$$

$$\begin{aligned} [\bar{1} \ 0 \ 1]_\gamma & \parallel [-0.920611 \ -1.062637 \ 1.084959]_{\alpha'} \\ (1 \ 1 \ 1)_\gamma & \parallel (0.015921 \ 0.978543 \ 0.971923)_{\alpha'} \end{aligned}$$

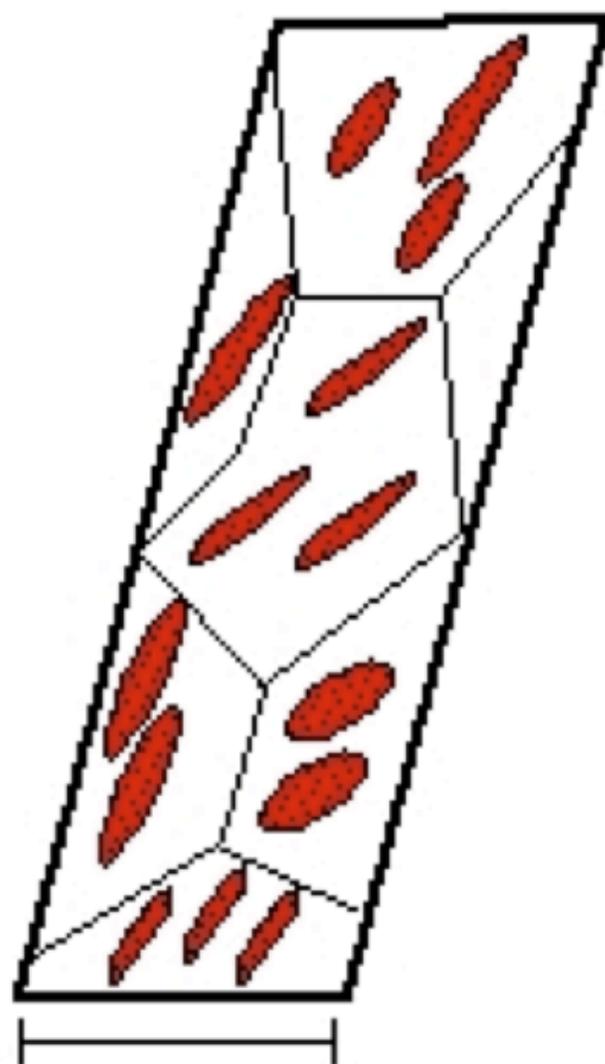
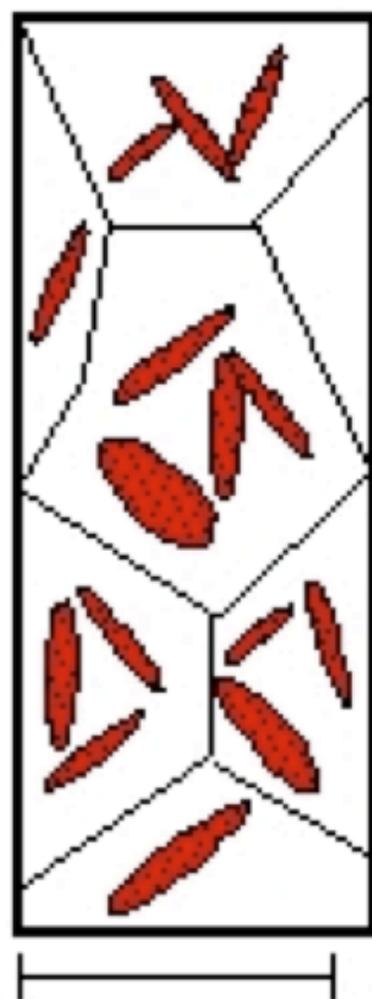
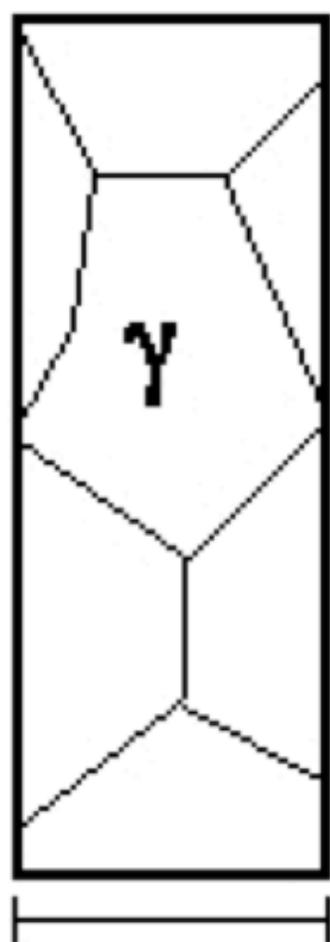
Shape change (γ P γ)

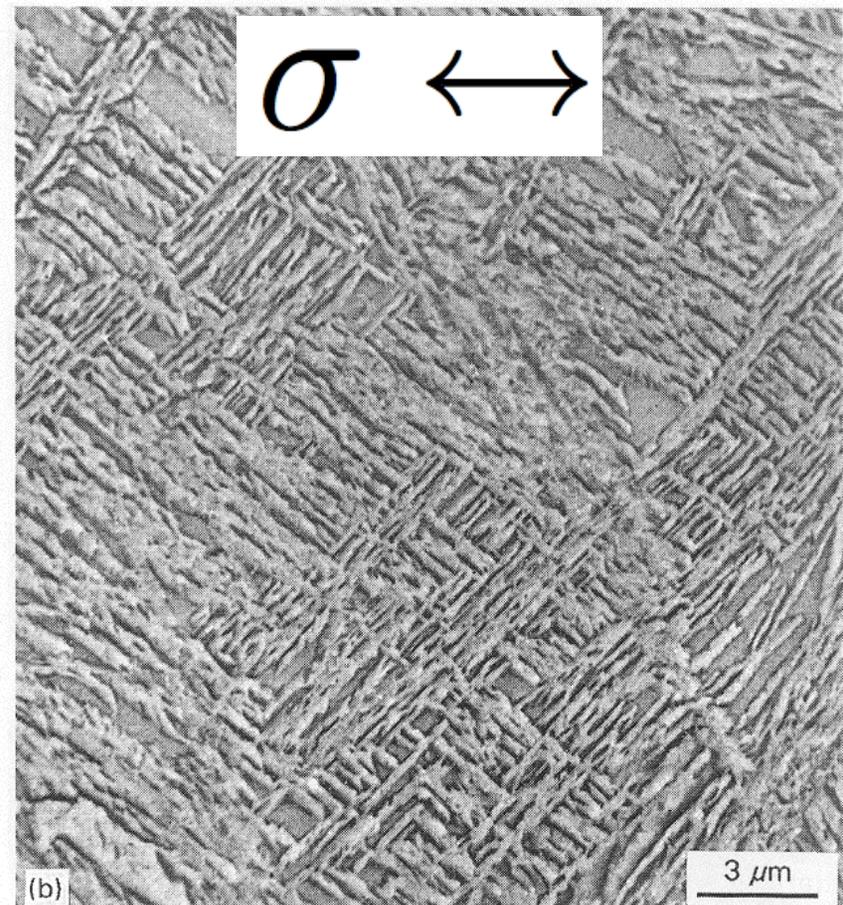
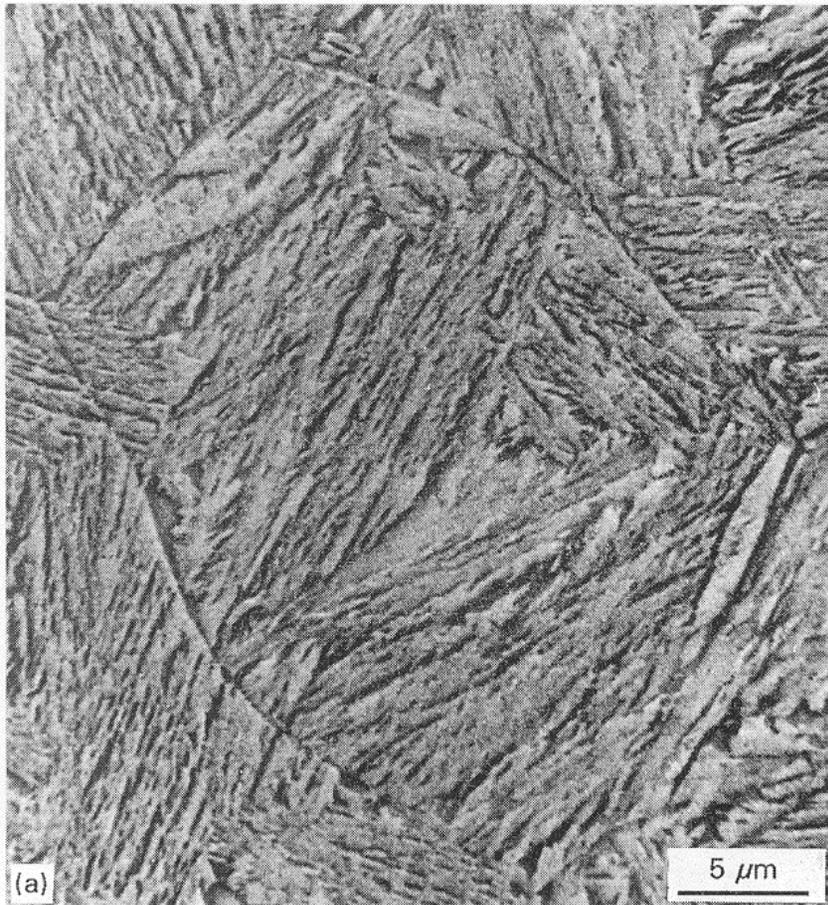
$$\begin{pmatrix} 0.992654 & -0.033124 & -0.027321 \\ 0.026378 & 1.118936 & 0.098100 \\ -0.027321 & -0.123190 & 0.898391 \end{pmatrix}$$





$$\Delta G_{MECH} = \tau s + \sigma_N \delta$$

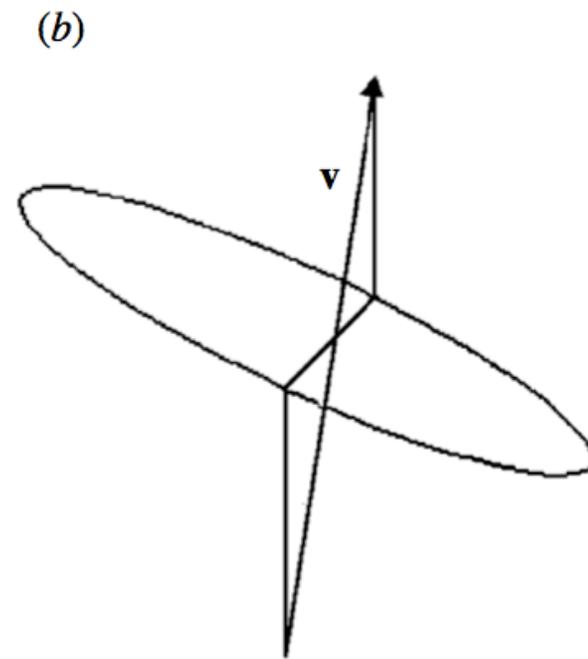
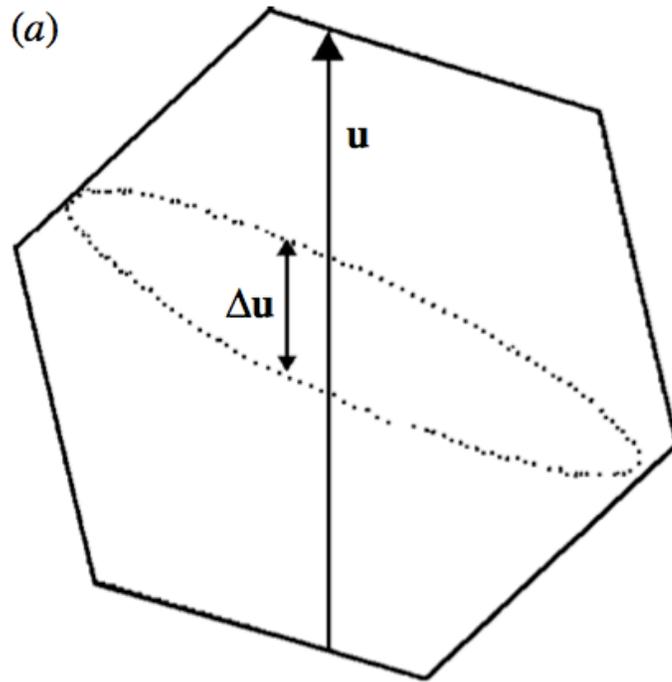




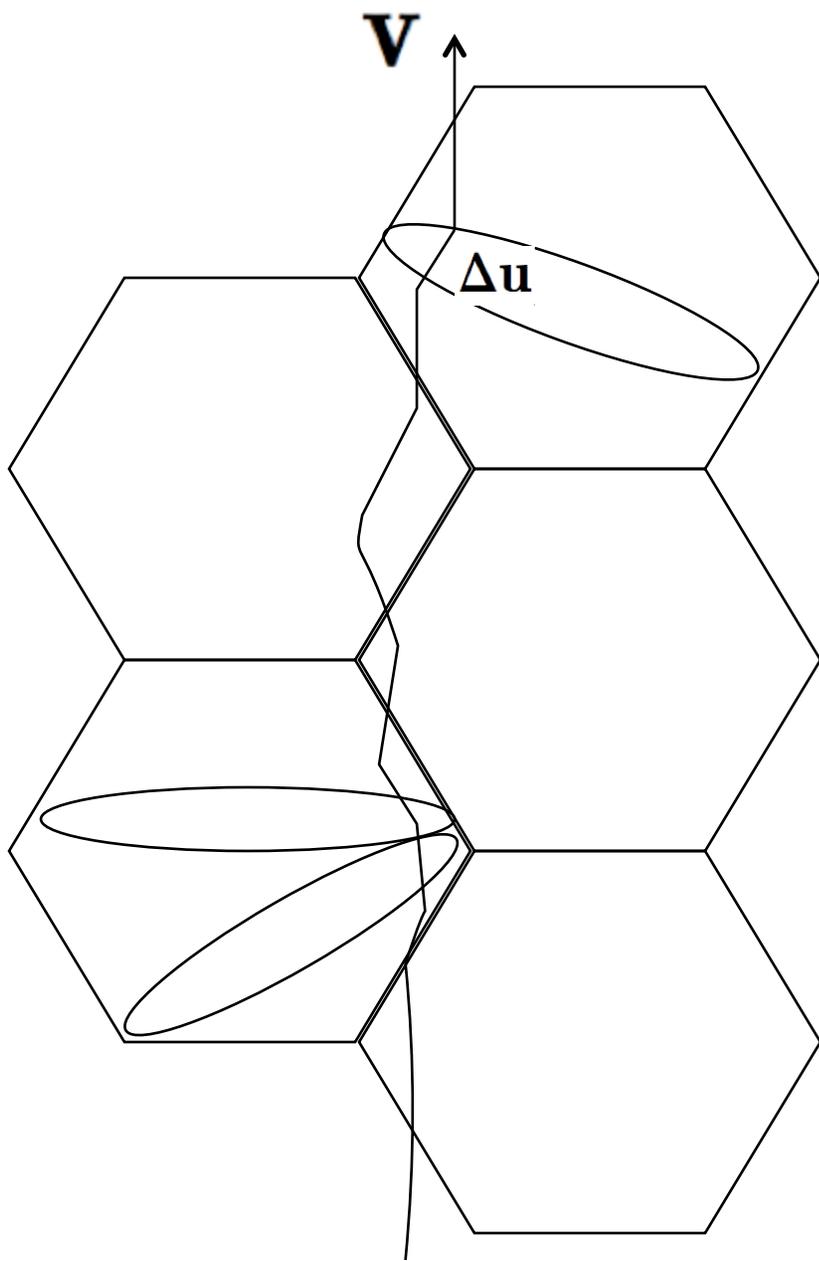
Lower bainite, transformed
with and without stress

Chang et al., 1996

$$(\mathbf{F} \mathbf{P} \mathbf{F}) = \mathbf{I} + m[\mathbf{F}; \mathbf{d}](\mathbf{p}; \mathbf{F}^*)$$



$$\mathbf{v} = \mathbf{P} \Delta \mathbf{u} + (\mathbf{u} - \Delta \mathbf{u})$$

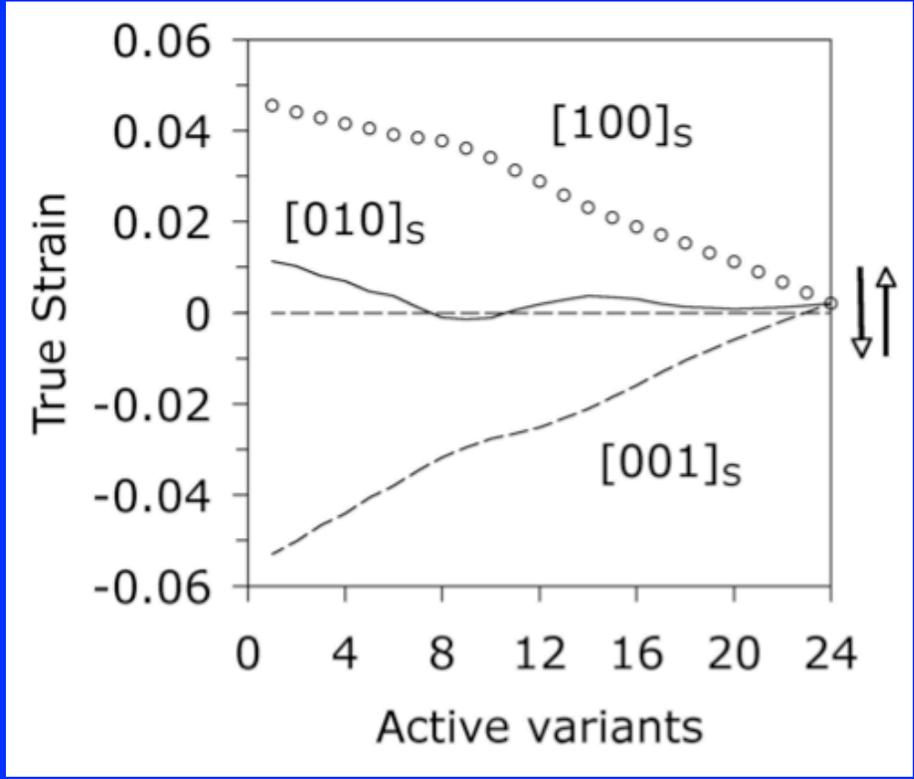
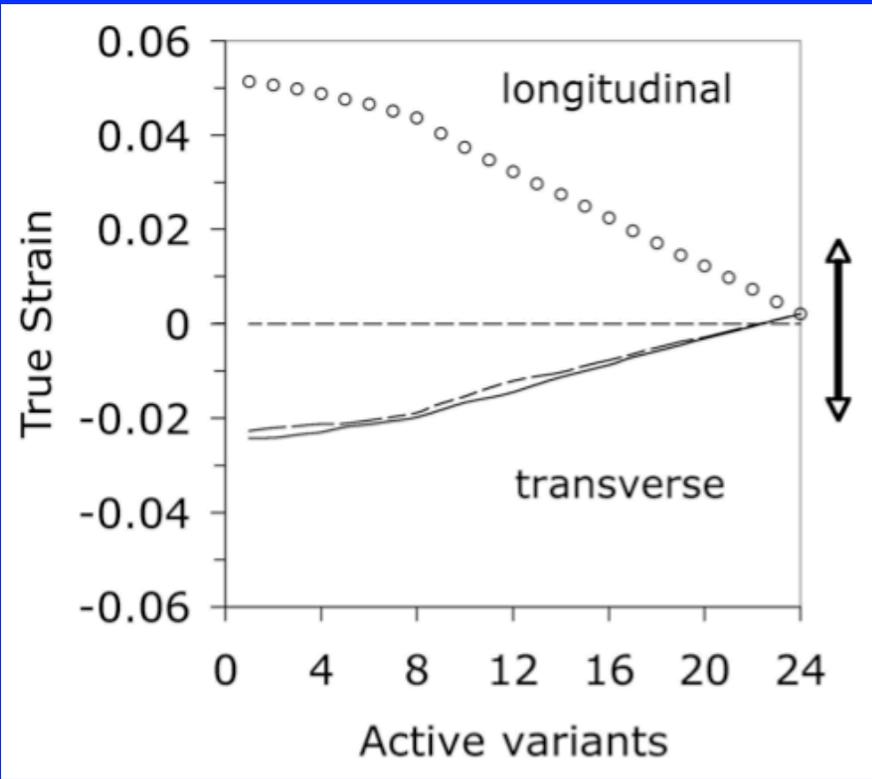


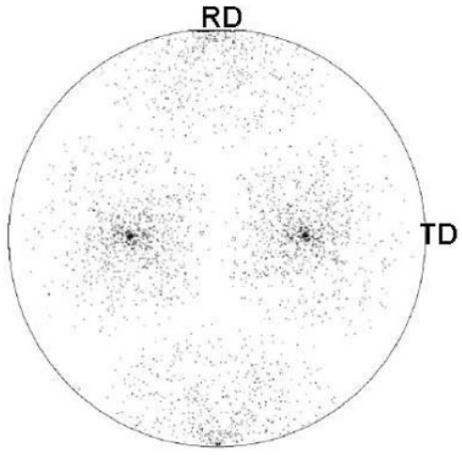
$$\ln\{|\mathbf{v}|/|\mathbf{u}|\}$$

$$\mathbf{v} = \sum_{k=1}^n \sum_{j=1}^{24} \mathbf{P}_j^k \Delta \mathbf{u}_j^k + \left(\mathbf{u} - \sum_{k=1}^n \sum_{j=1}^{24} \Delta \mathbf{u}_j^k \right)$$

24 crystallographic variants

n austenite grains



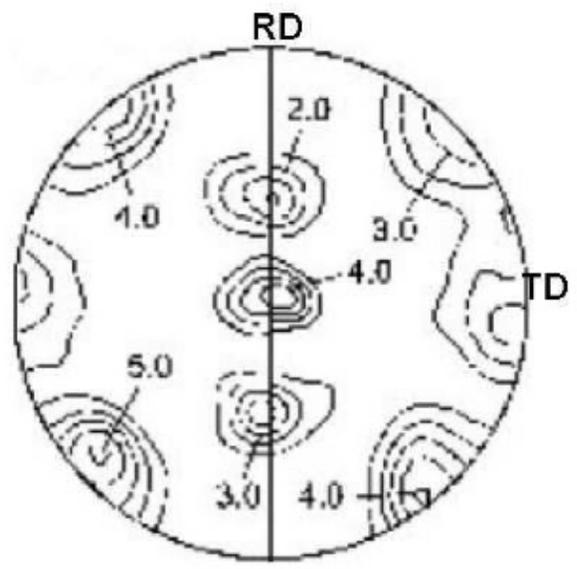


Goss

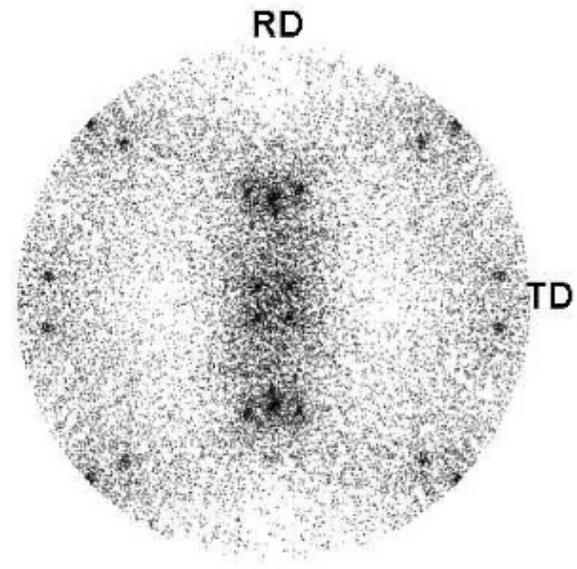
Experimental

Calculated

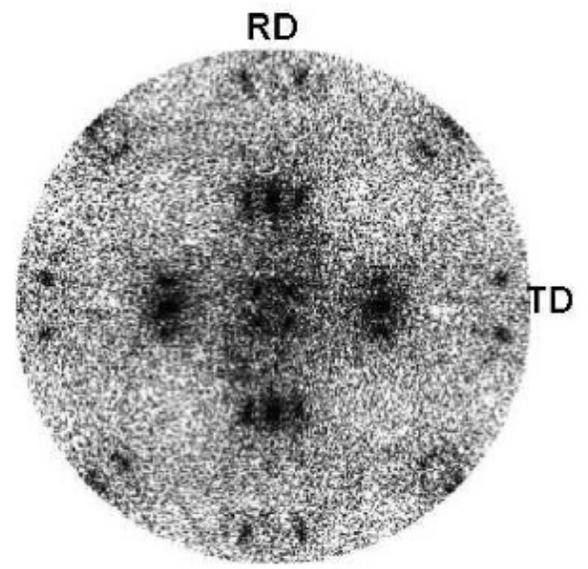
Calculated



(a)

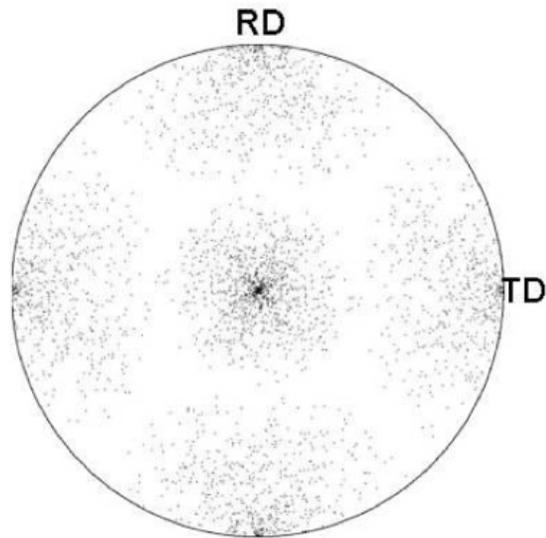


(b)



(c)

Kundu and Bhadeshia, Scripta Materialia 55 (2006) 779

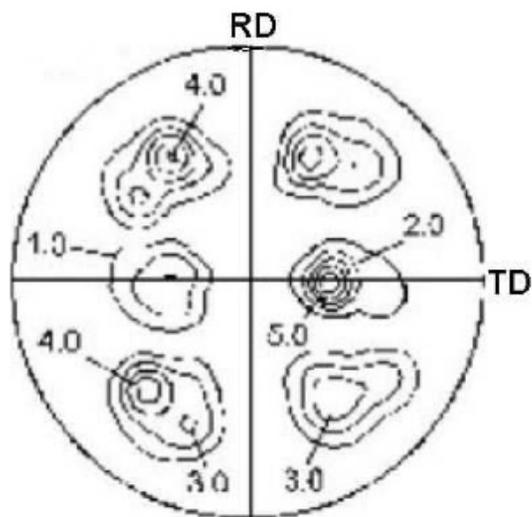


Cube

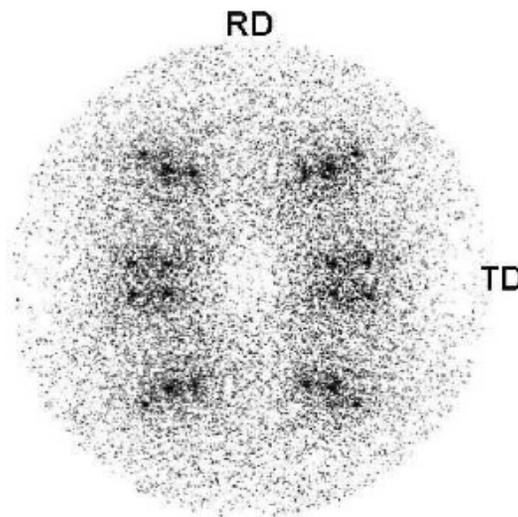
Experimental

Calculated

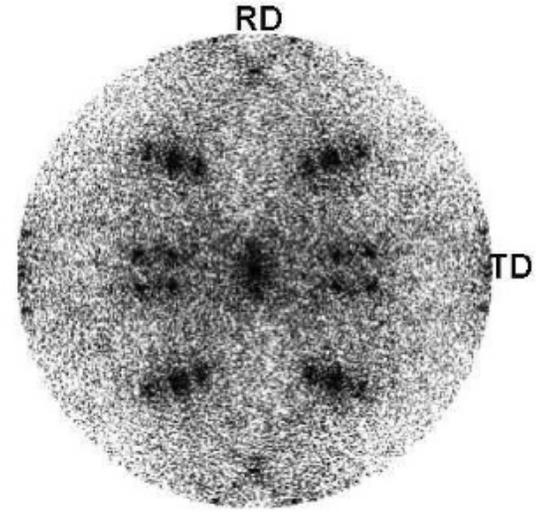
Calculated



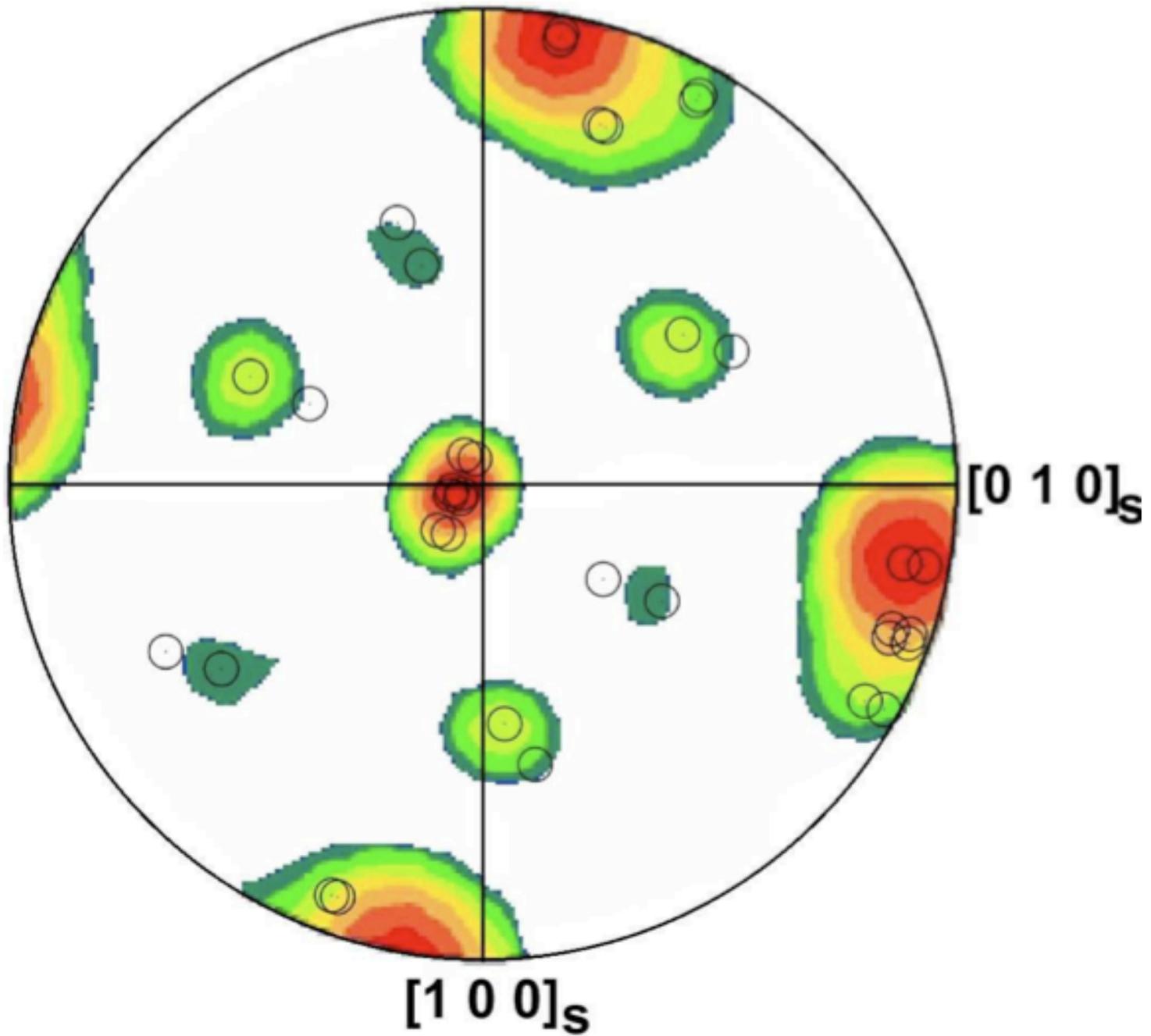
(a)



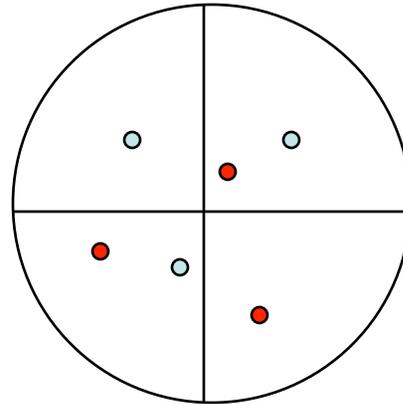
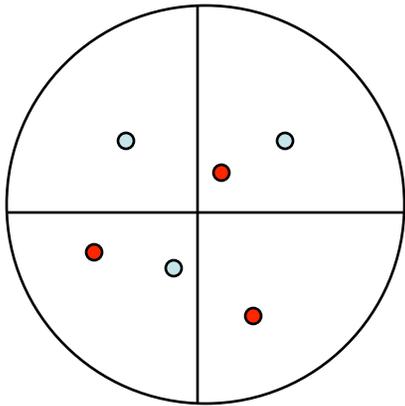
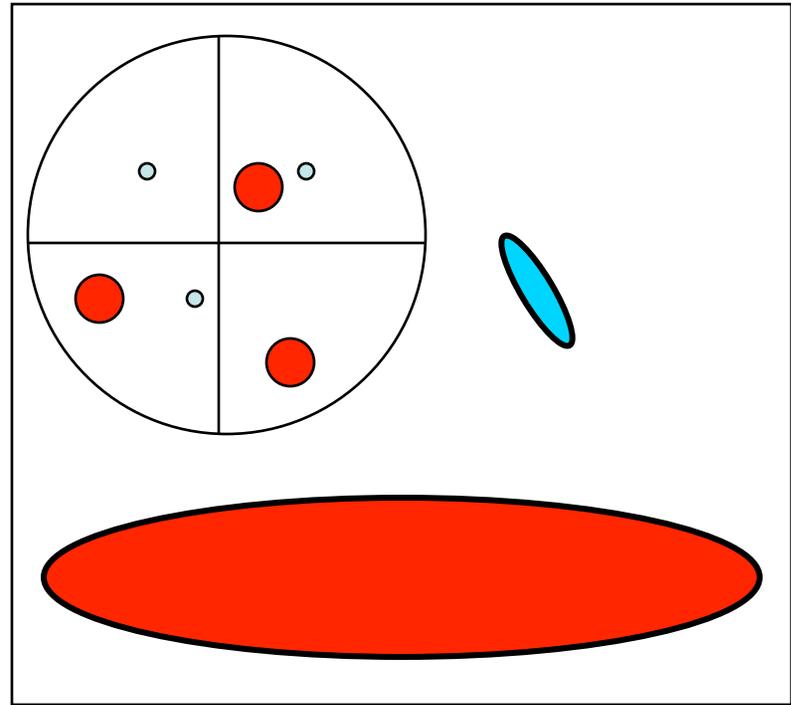
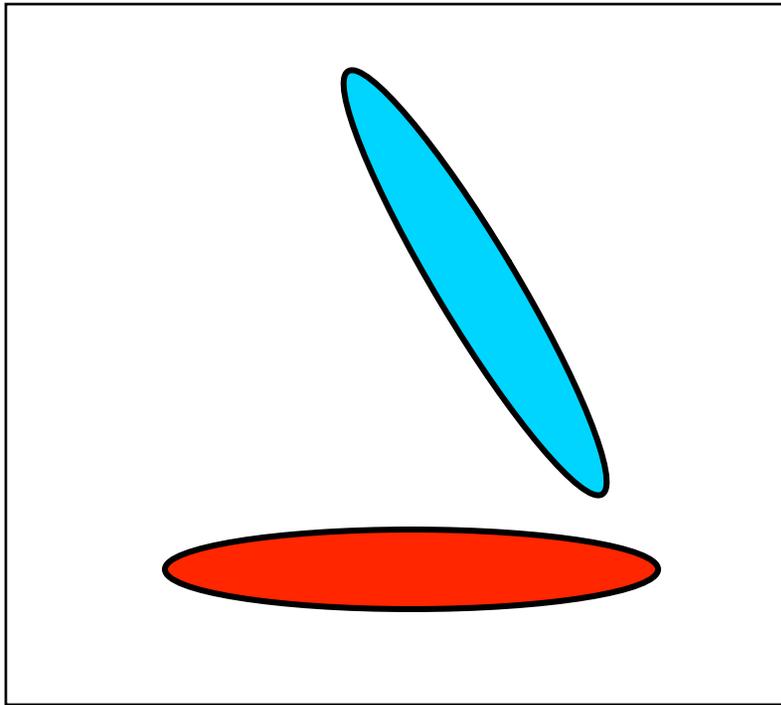
(b)



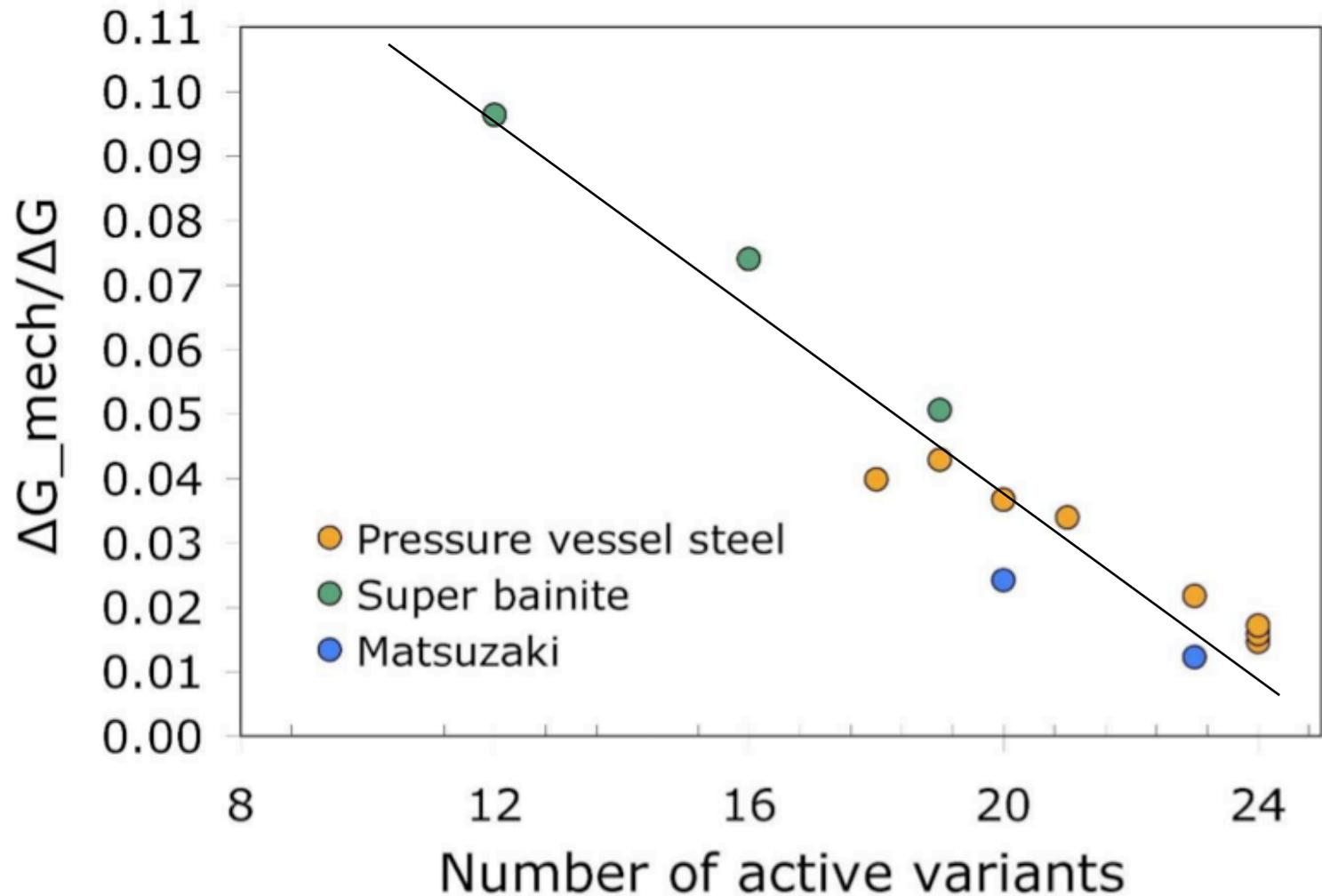
(c)



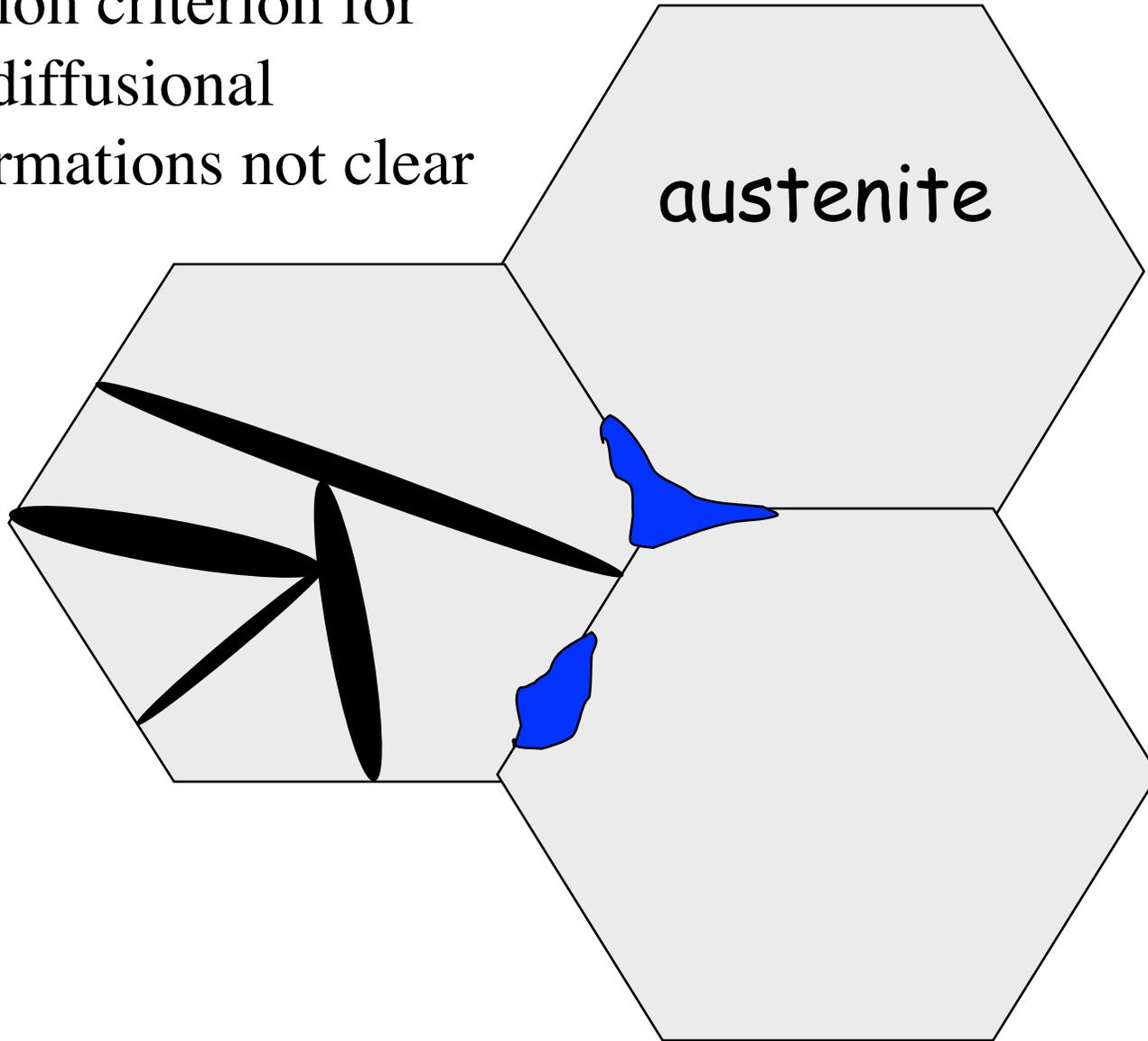
No method calculates **INTENSITY**,
only **POSITIONS** of poles

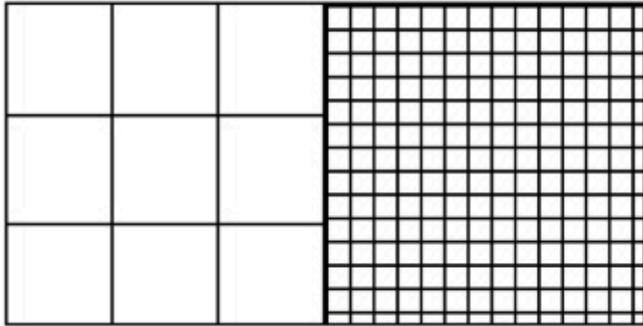


$$\Delta G = \Delta G_{CHEM} + \Delta G_{MECH}$$

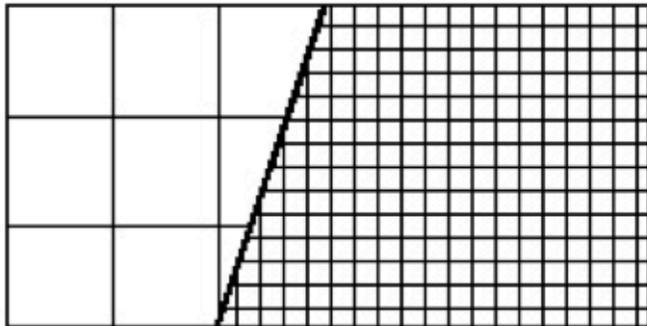


selection criterion for
diffusional
transformations not clear

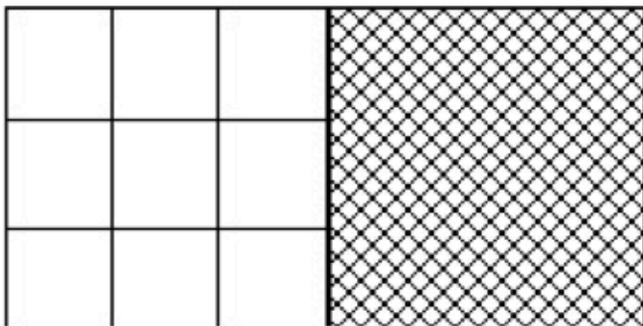




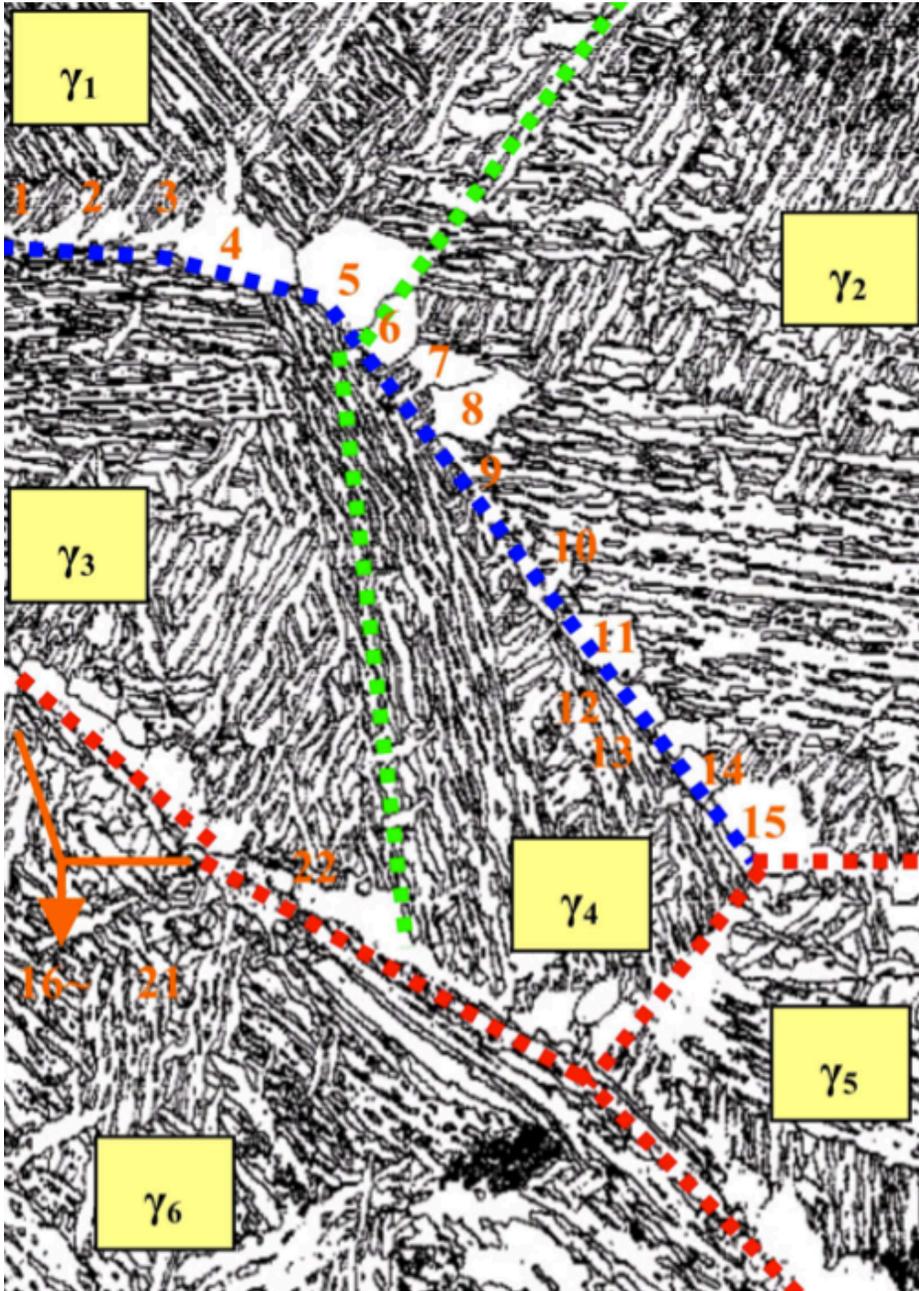
Reference
bicrystal



Orientations fixed,
interface plane altered



Orientation altered,
interface plane fixed



Contact with more than one austenite grain

Role of austenite grain boundary plane

Nucleation or growth dominated?

Number of variables very large ($10 \mu\text{m}$ cube requires 10^{15} parameters)